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## **APPENDIX – A**

### **SELECTION OF SEISMIC RETROFITTING CATEGORY**



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## **APPENDIX – B**

**PREPARATION OF BRIDGE MODEL USING SAP 2000 VR. 14.1.0**



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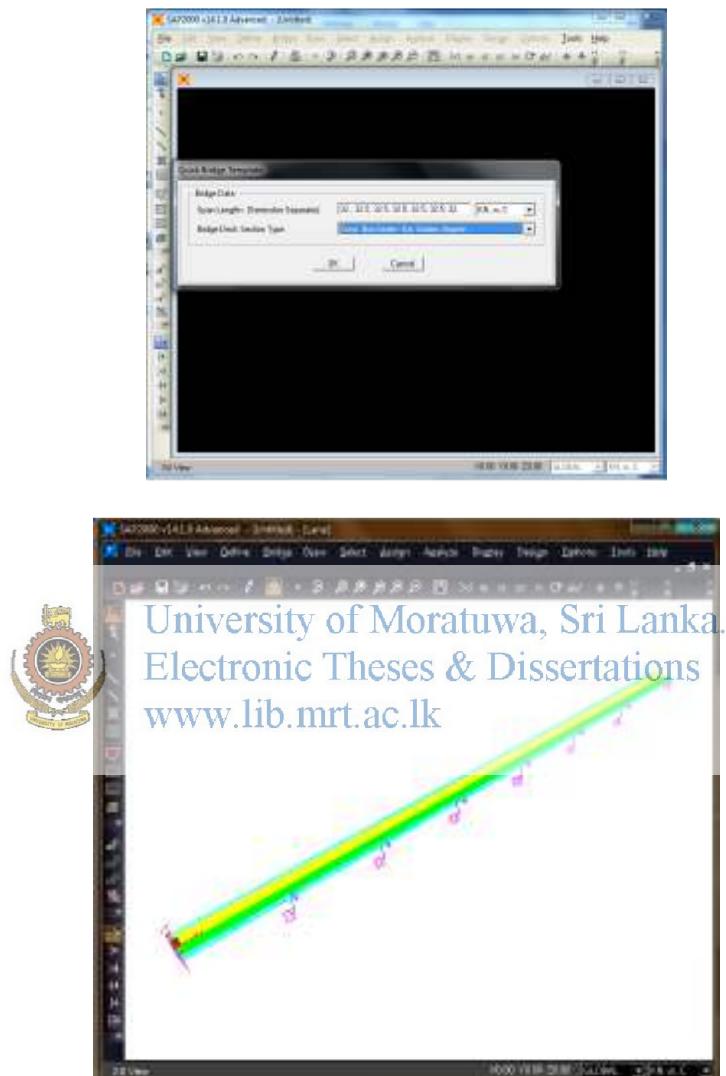
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## PREPARATION OF BRIDGE MODEL USING SAP 2000 Vr. 14.1.0

### **Some Important Steps of Building of the FEM**

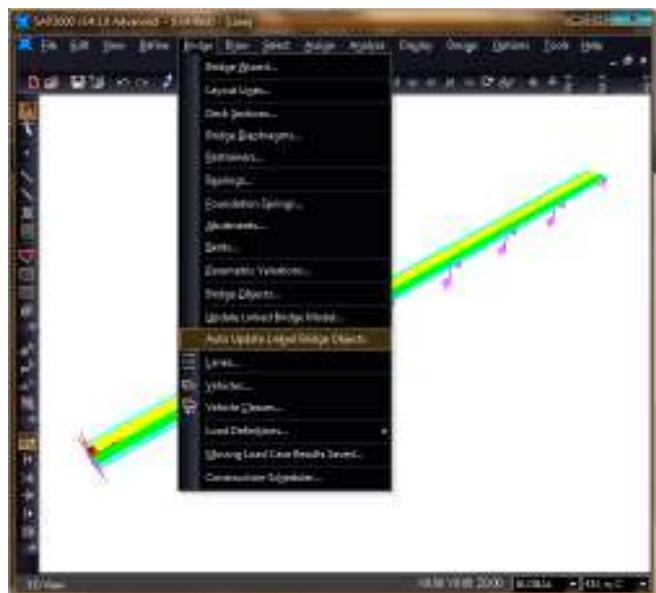
SAP 2000 version 14.1.0 was used to prepare the bridge model.

File → New Model → Quick Bridge

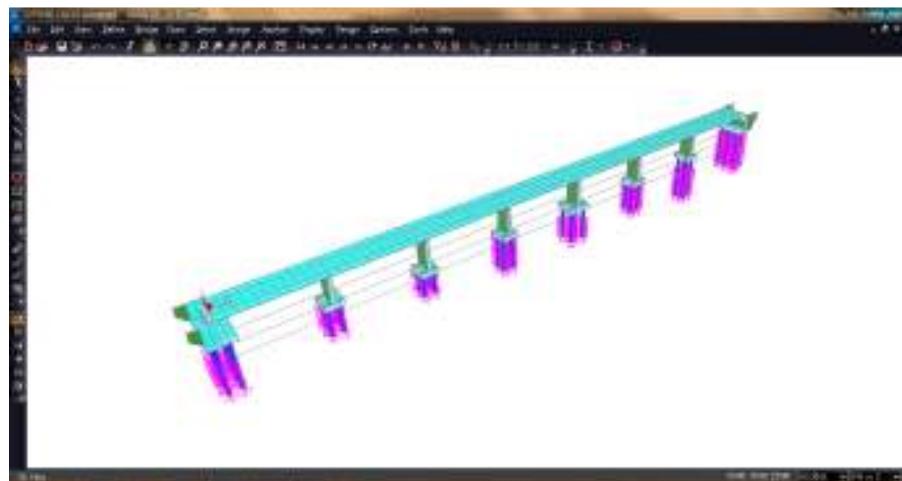
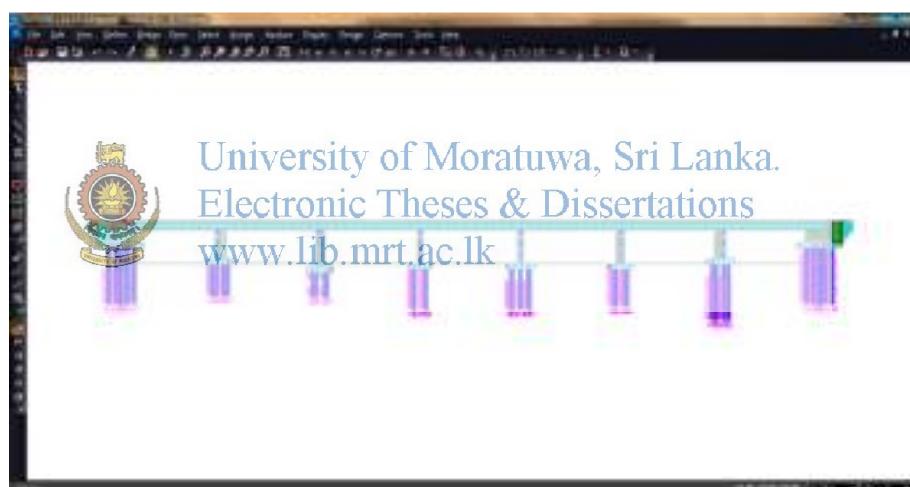


Once it is prepared the primary modal the geometry and the material properties can be changed as you wish using Bridge wizard. In the bridge modeler wizard, it can be defined and modified all the material properties, section properties and also it can be assigned the same.

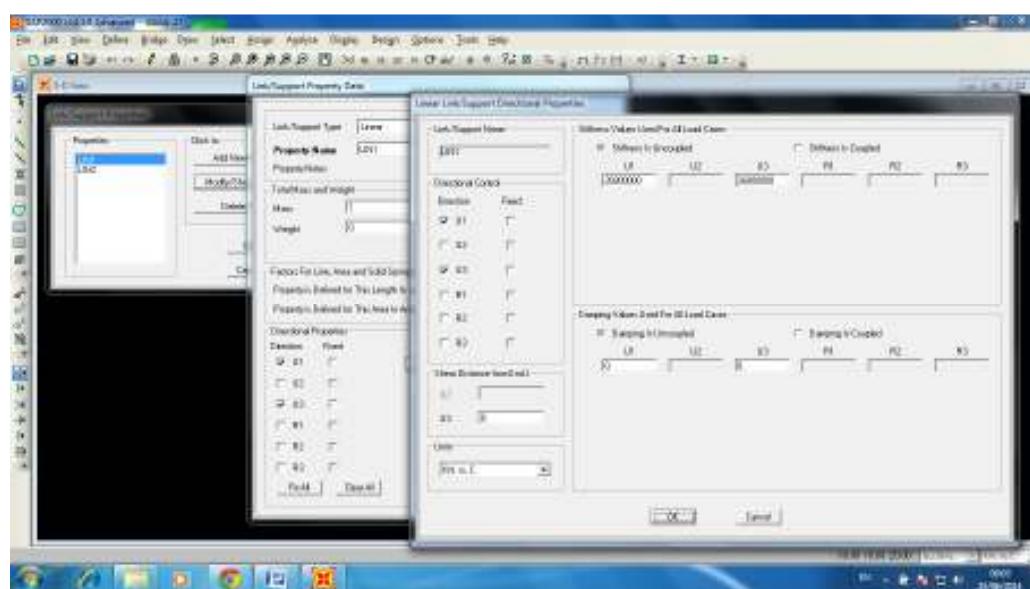
In this case study, only the superstructure was defined using the bridge wizard and substructure was defined and connected to the superstructure manually using area elements (for pile caps, abutments, piers and wing walls), frame elements (for abutment cap, pier cap and piles) and link elements (for bearings). Also make sure to offline the “Auto update linked bridge objects” in the bridge menu of the SAP 2000.



After completing model building, it was as follows.



When it defines the link object properties to define the bearings, two objects were defined to get the fixed and free connections.



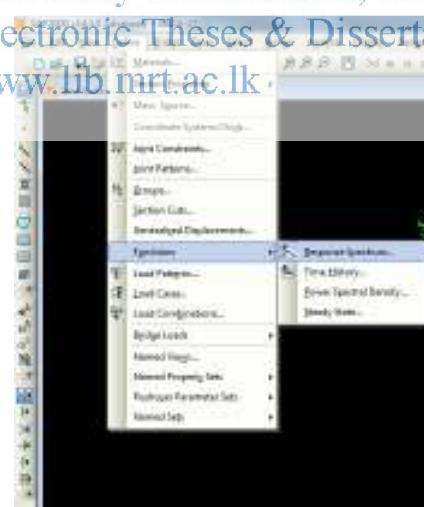
Soil properties were assigned to the model using springs. The values of the springs were taken using the N values (1500N). The N values were extracted from the as built drawings. The drawing was annexed.

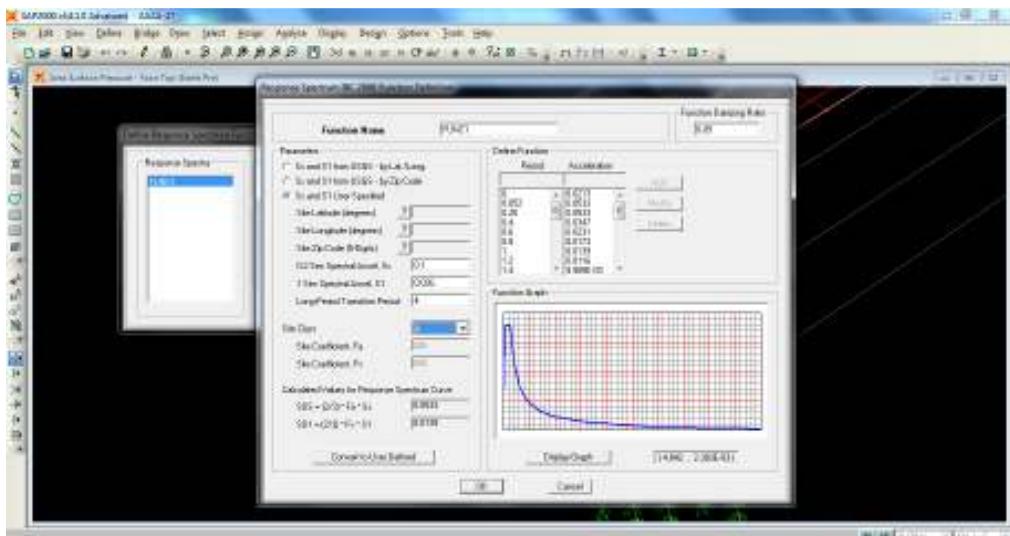


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**Load Case Data - Modal**

Load Case Name: MODAL      Notes: Modify/Show...      Load Case Type: Modal

Stiffness to Use:

- Zero Initial Condition - Unstressed State.
- Stiffness of End of Nonlinear Case

Important Note: Loads from the Nonlinear Case are NOT included in the current case.

Number of Nodes:

Maximum Number of Nodes: 50      Minimum Number of Nodes: 1

Load Applied:

Load Type	UT	Target Dynamic	Participation Factor
Load Code	0.1g	GRCS	0.00
Accel	UT	0.0	0.00
Accel	UT	0.0	0.00

Add      Modify      Delete      OK      Cancel

**Load Case Data - Response Spectrum**

Load Case Name: PGK.0.1g      Notes: Modify/Show...      Load Case Type: Response Spectrum

Modal Combination:

- CQC      GNC 1: 1
- SRSS      GNC 2: 0
- Absolute
- GRCS
- NRC 10 Percent
- Double Sum

Directional Combination:

- SRSS
- Absolute
- Scale Factor: [ ]

Modal Load Case:

Use Modes from this Modal Load Case: MODAL

Load Applied:

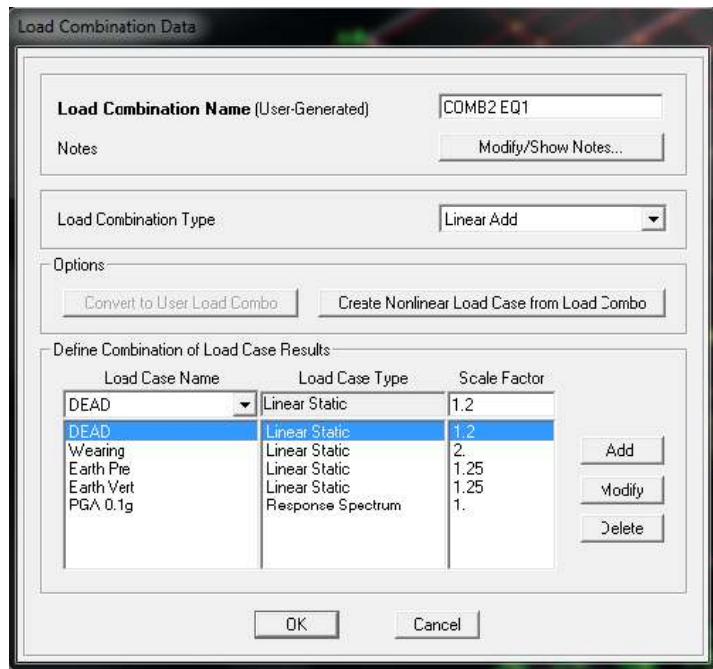
Load Type	Load Name	Function	Scale Factor
Accel	UT	FUNCT1	1
Accel	UT	FUNCT1	1

Add      Modify      Delete

Show Advanced Load Parameters

Other Parameters:

Modal Damping: Constant at 0.05      Modify/Show...      OK      Cancel



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## **APPENDIX – C**

**RESULTS OBTAINED FROM BRIDGE MODEL DEVELOPED USING**



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## RESULTS OBTAINED FROM BRIDGE MODEL DEVELOPED USING SAP 2000 Vr. 14.1.0

### Modal Analysis

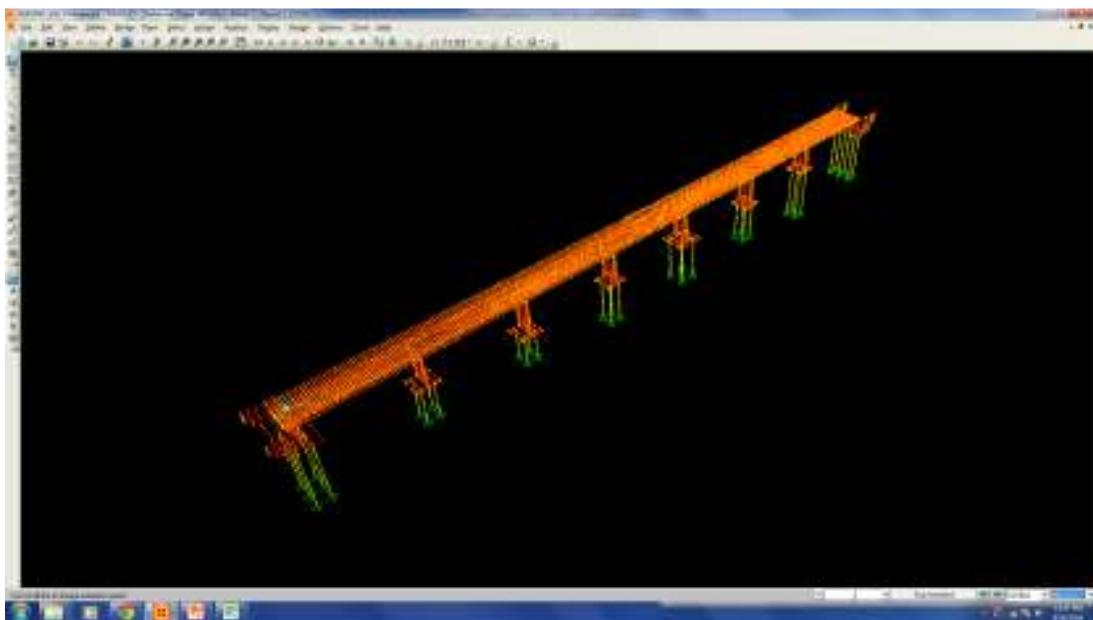


Fig Aiii-1; Mode No.1 – translation mode



Fig Aiii-2; Mode No.8 – Bending mode

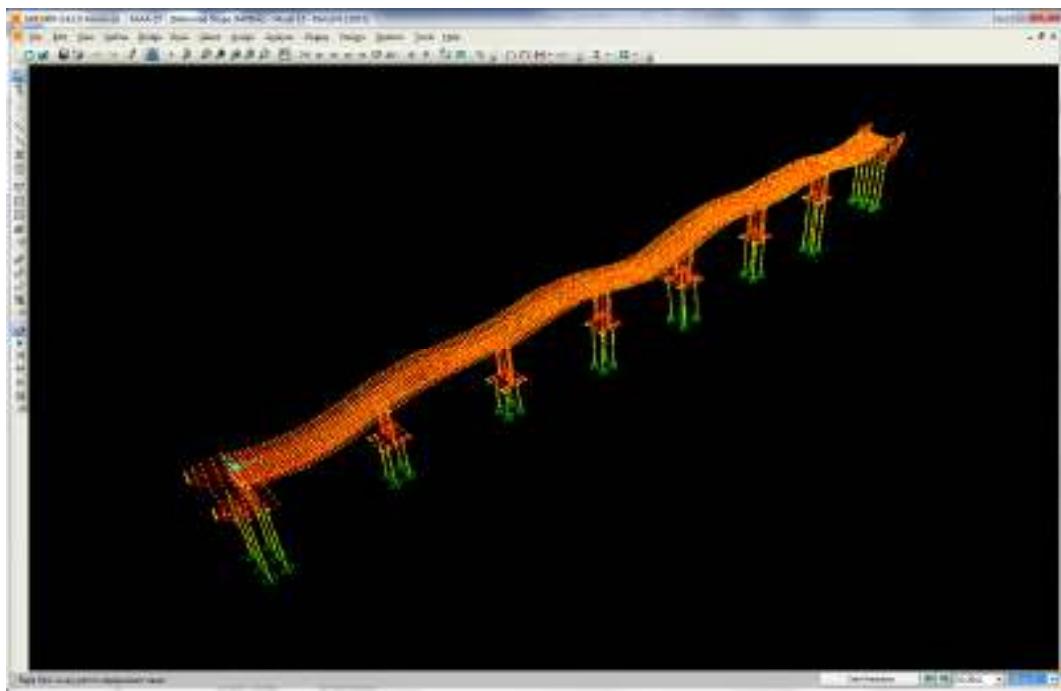


Fig Aiii-3; Mode No.12 – Bending mode

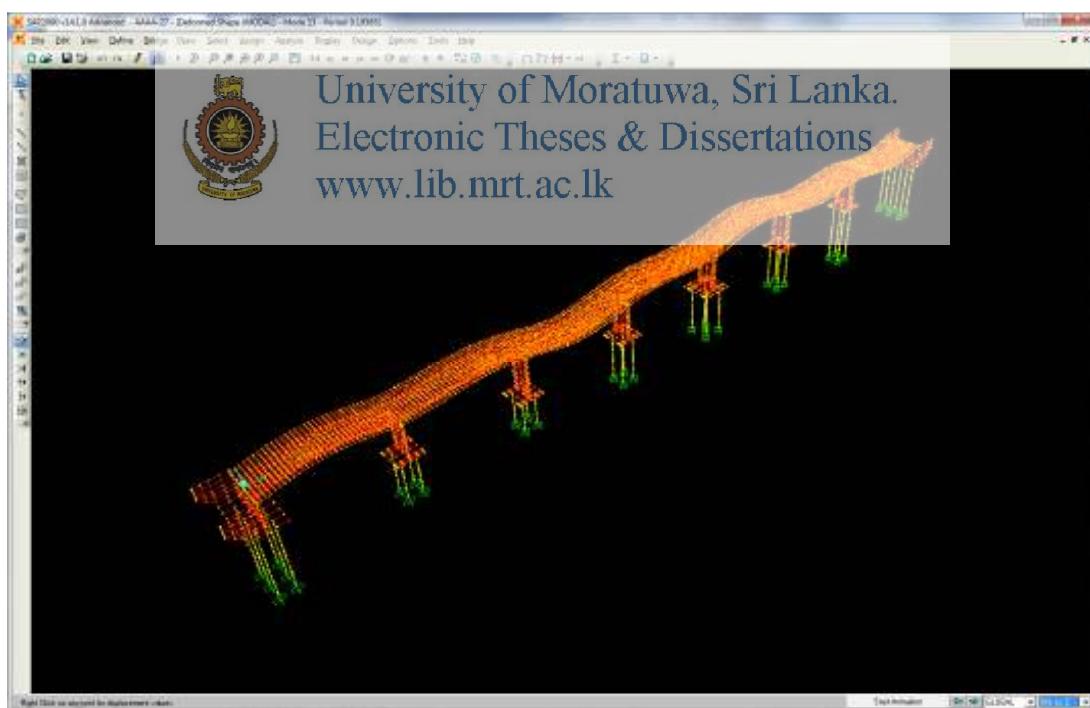


Fig Aiii-4; Mode No.13 – Bending mode

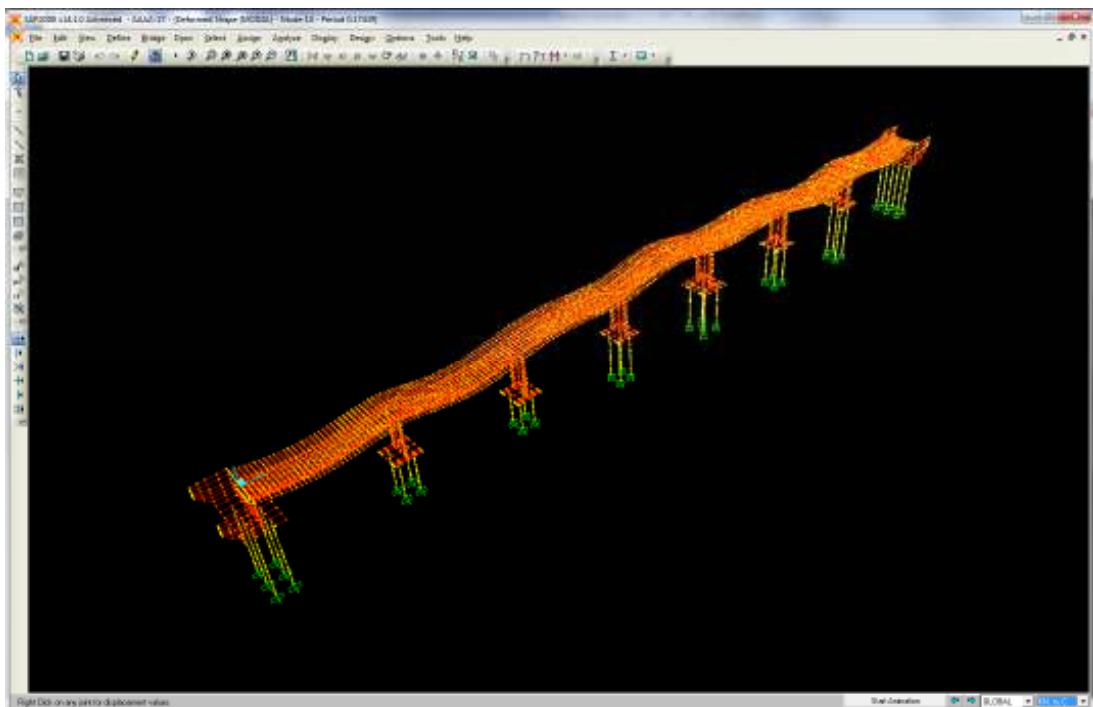


Fig Aiii-5; Mode No.14 – Bending mode

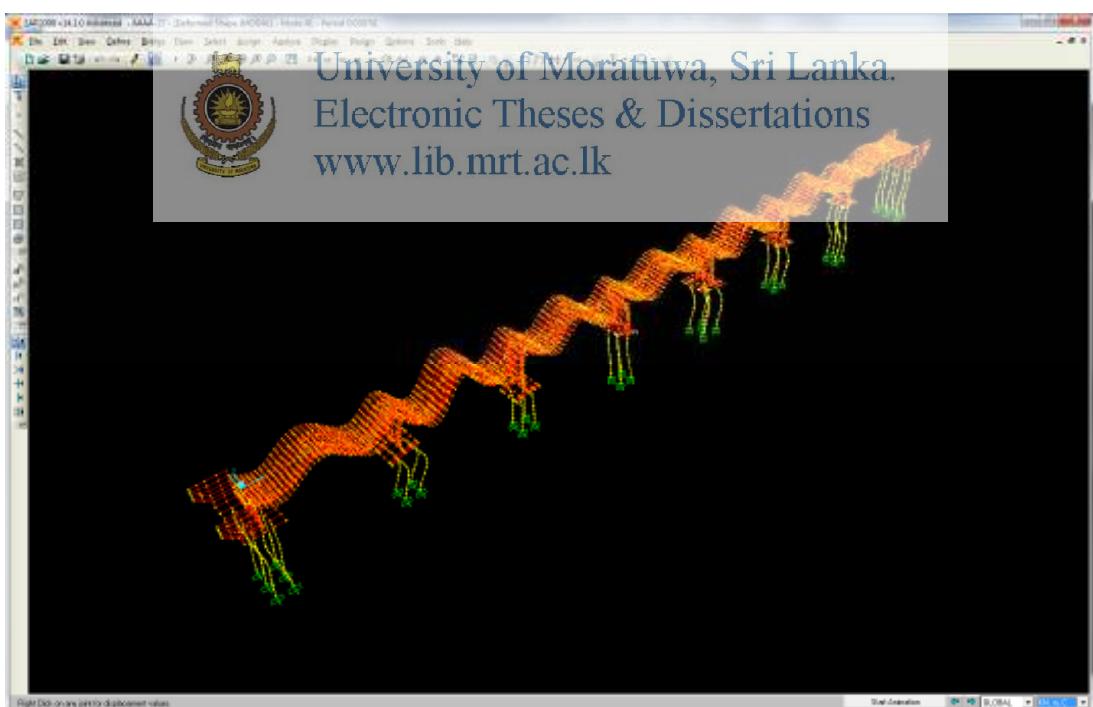


Fig Aiii-6; Mode No.41 – Bending mode

## Results (Superstructure)

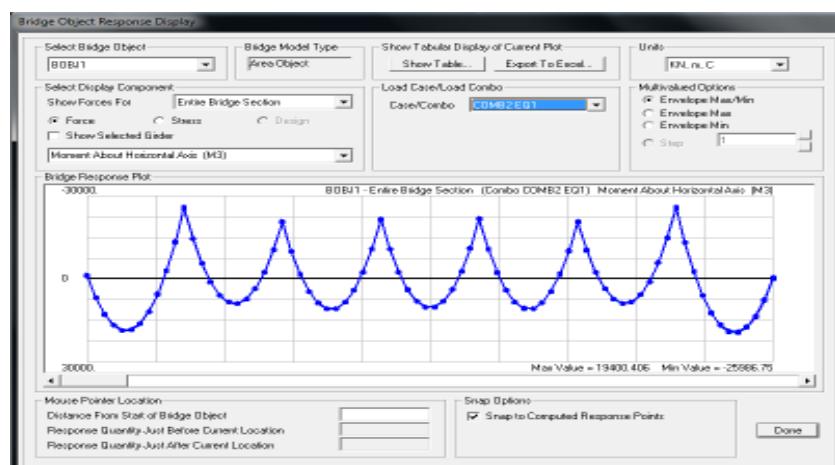


Fig Aiii-7; Bending moment envelope (Com2 EQ1)

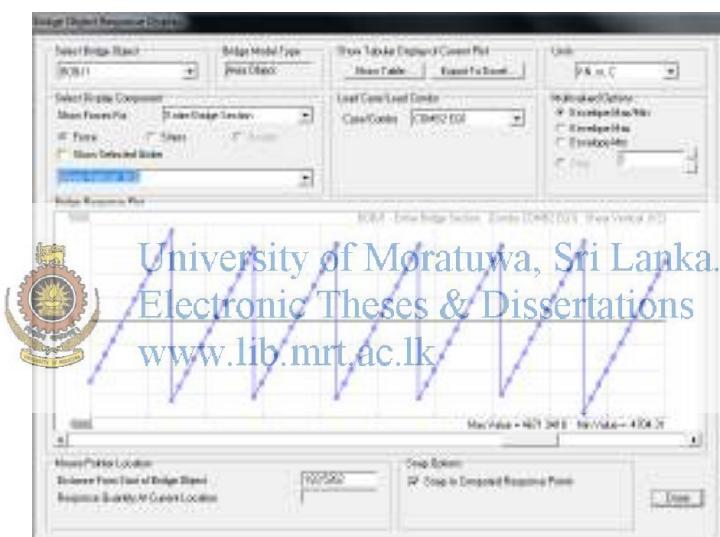


Fig Aiii-8; Shear force envelope (Com2 EQ1)

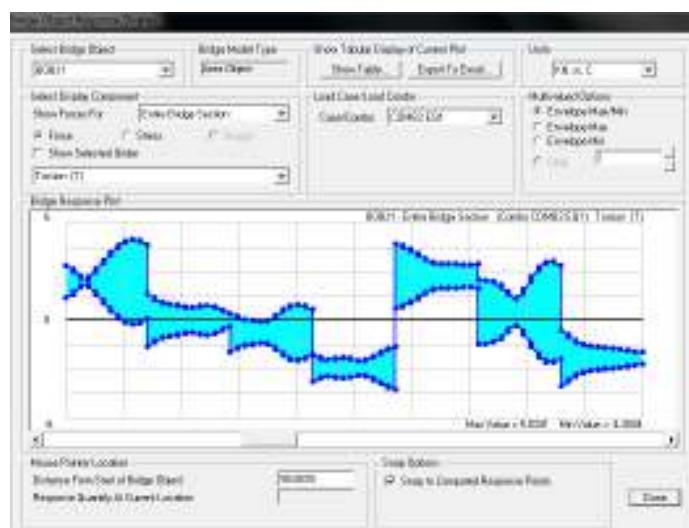


Fig Aiii-9; Torsion envelope (Com2 EQ1)

## Results (Substructure)

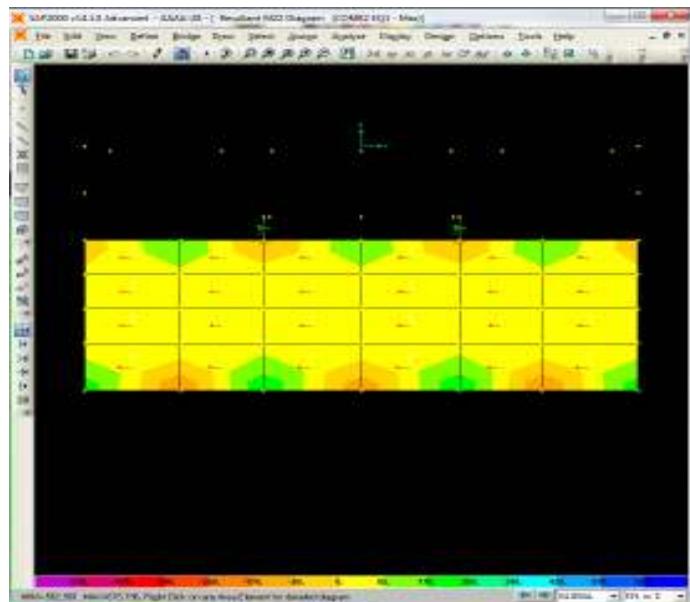


Fig Aiii-10; Bending moment distribution - Abutment A1 (Com2 EQ1)

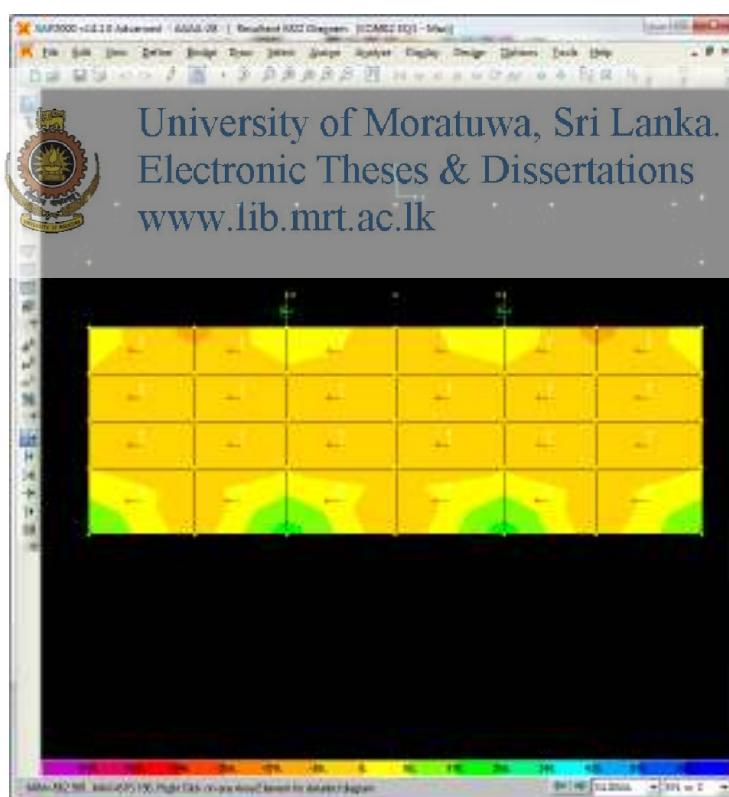


Fig Aiii-11; Bending moment distribution - Abutment A2 (Com2 EQ1)

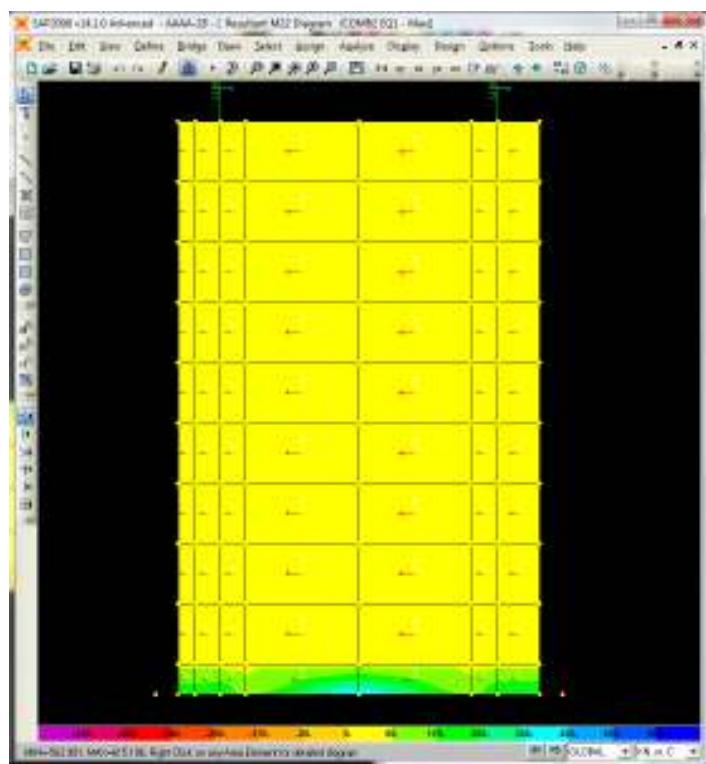


Fig Aiii-12; Bending moment distribution – Pier P1 (Com2 EQI)

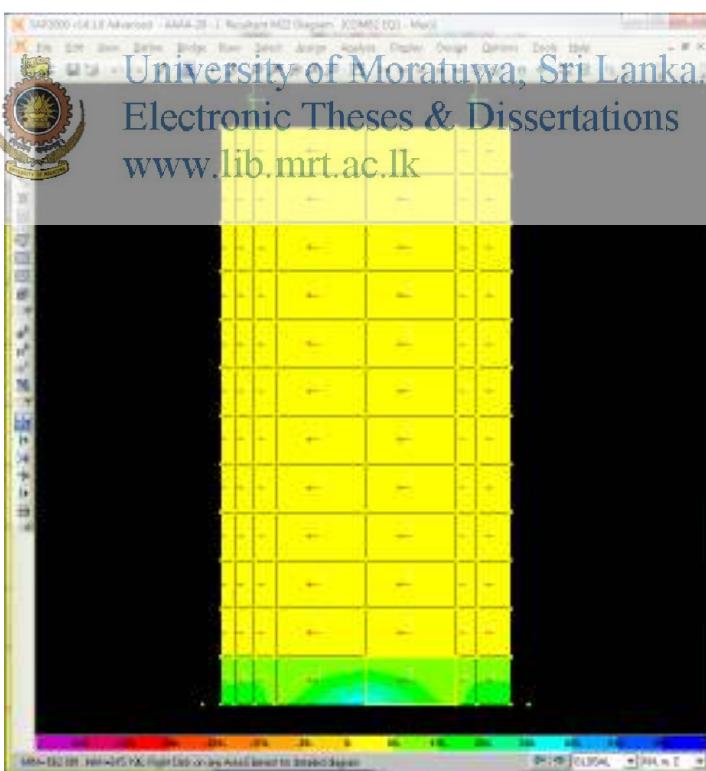


Fig Aiii-13; Bending moment distribution – Pier P2 (Com2 EQI)

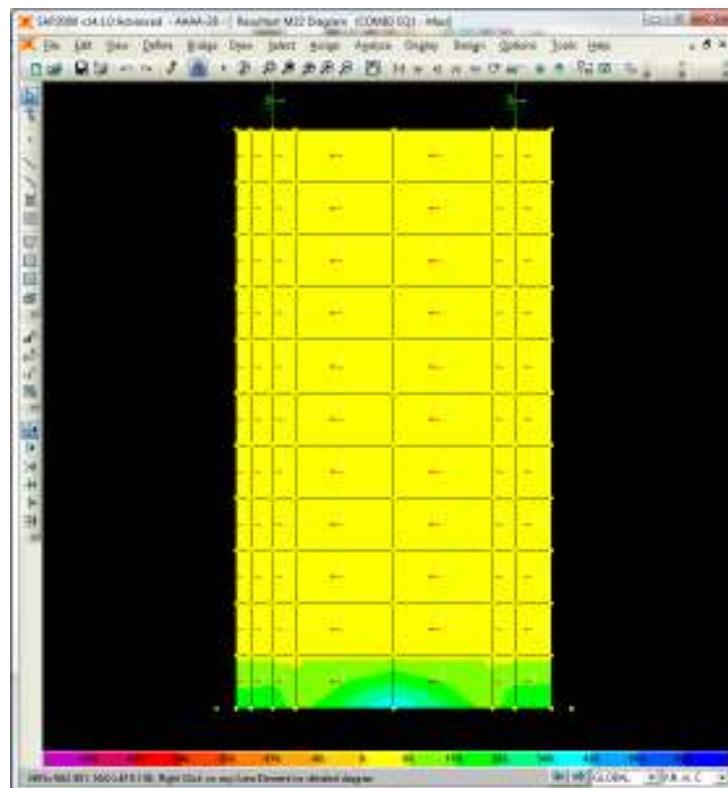


Fig Aiii-14; Bending moment distribution – Pier P3 (Com2 EQI)

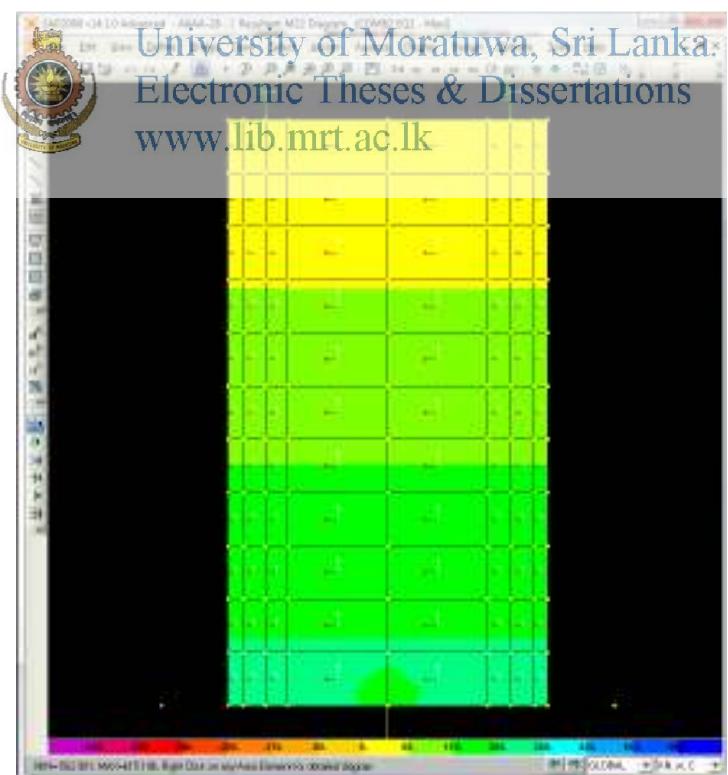


Fig Aiii-14; Bending moment distribution – Pier P4 (Com2 EQI)

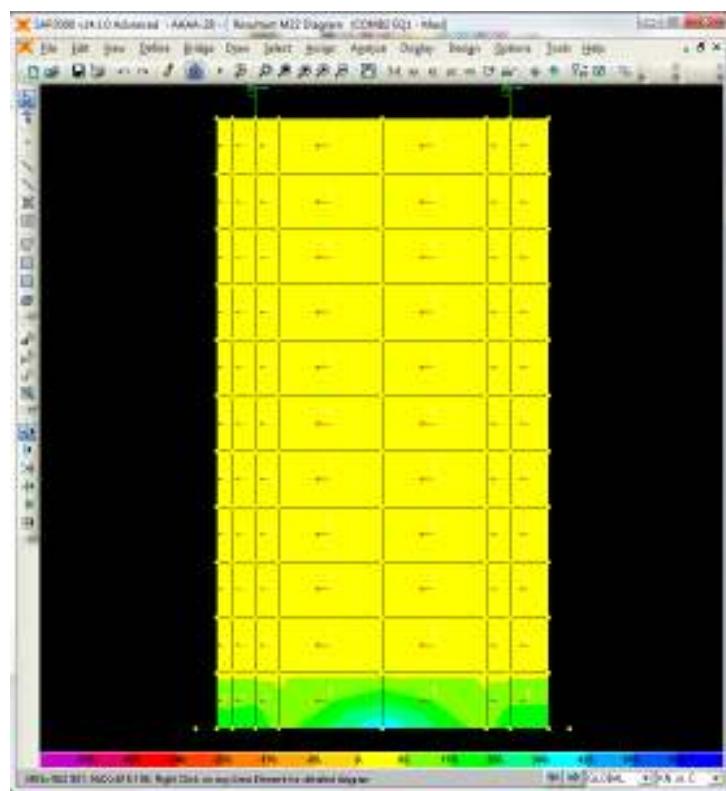


Fig Aiii-15; Bending moment distribution – Pier P5 (Com2 EQI)

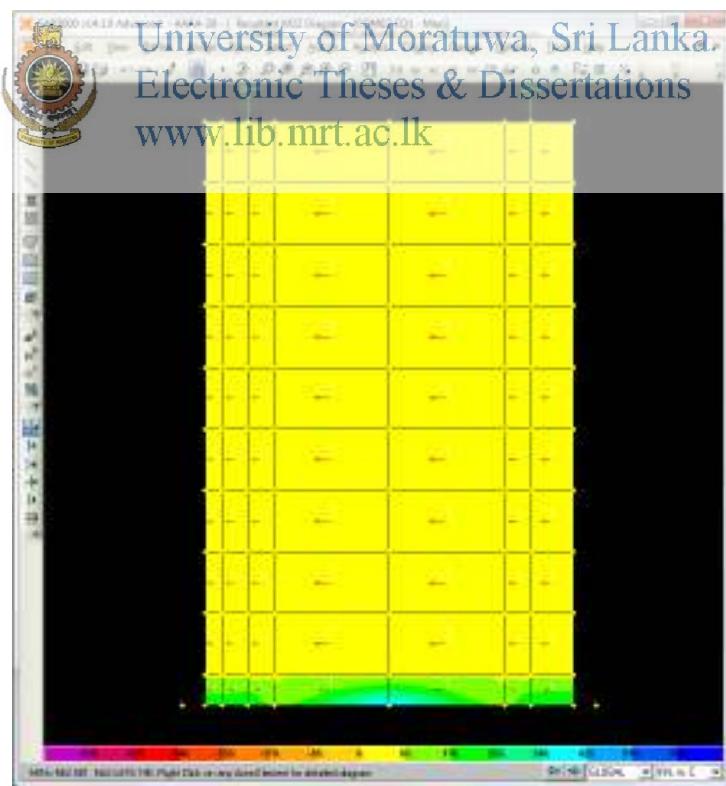


Fig Aiii-16; Bending moment distribution – Pier P6 (Com2 EQI)

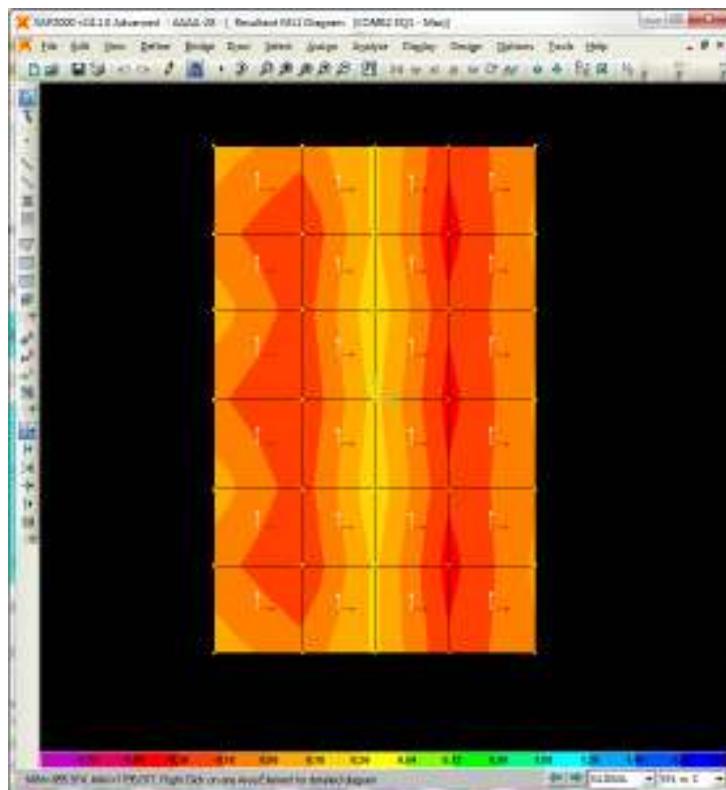


Fig Aiii-17; Bending moment distribution – Pile cap A1 (Com2 EQ1)

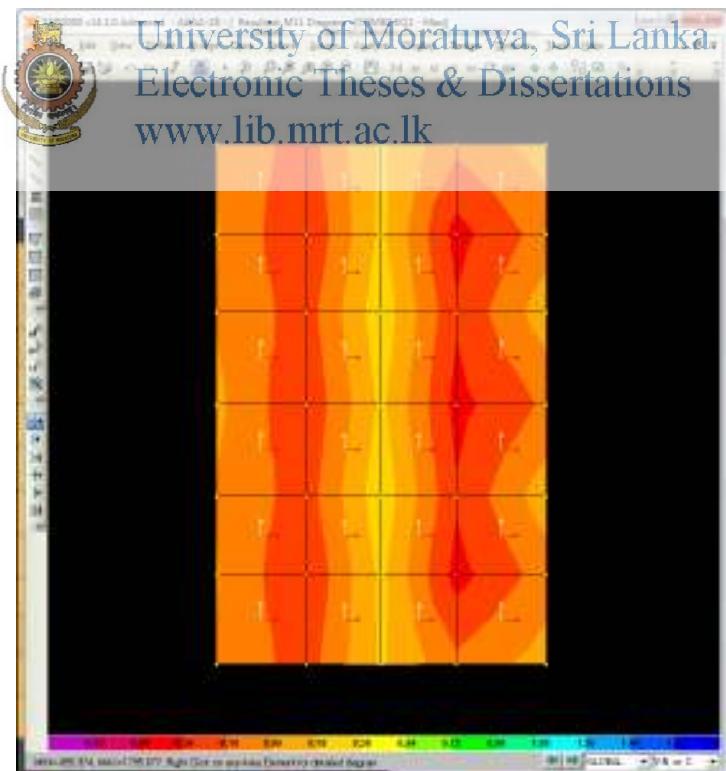


Fig Aiii-18; Bending moment distribution – Pile cap A2 (Com2 EQ1)

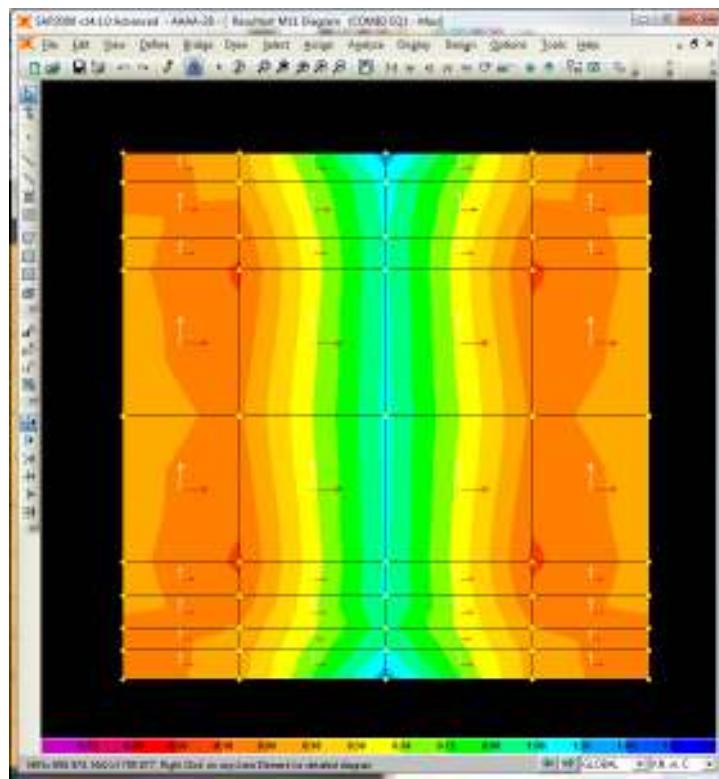


Fig Aiii-19; Bending moment distribution – Pile cap P1 (Com2 EQ1)

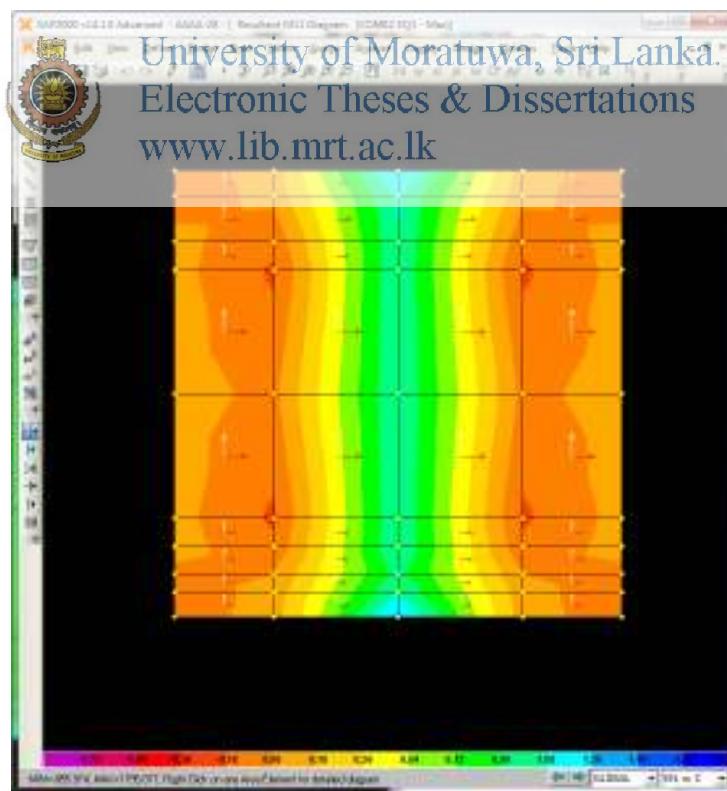


Fig Aiii-20; Bending moment distribution – Pile cap P2 (Com2 EQ1)

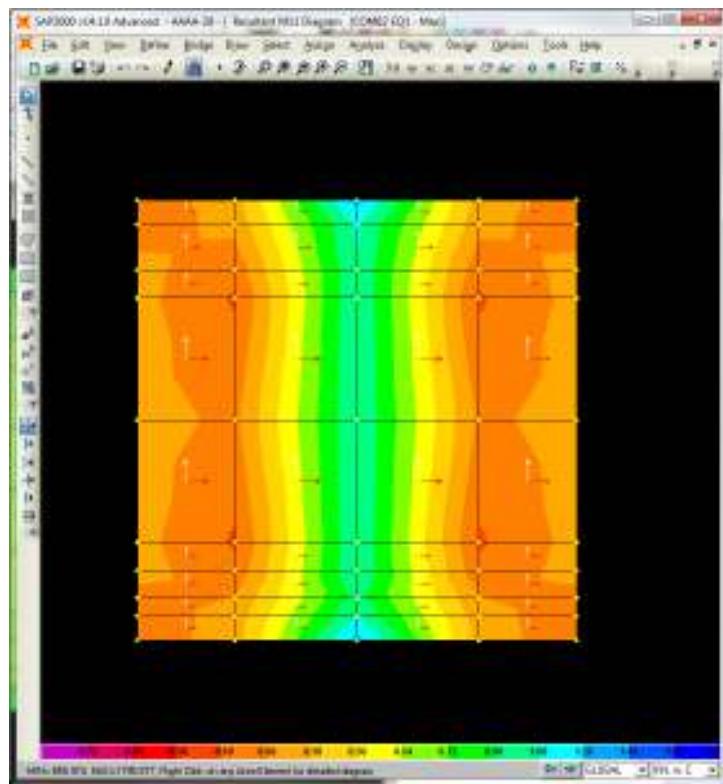


Fig Aiii-21; Bending moment distribution – Pile cap P3 (Com2 EQ1)

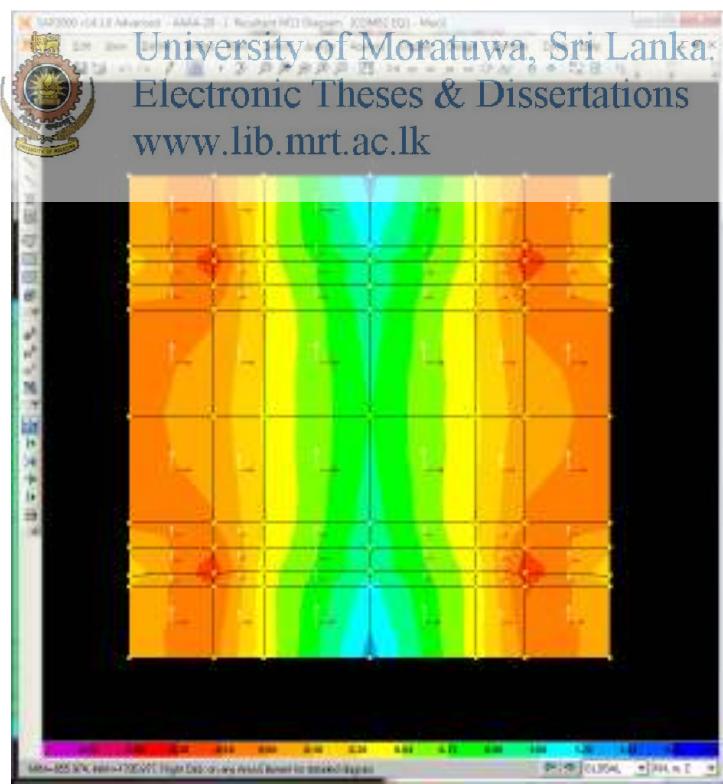


Fig Aiii-22; Bending moment distribution – Pile cap P4 (Com2 EQ1)

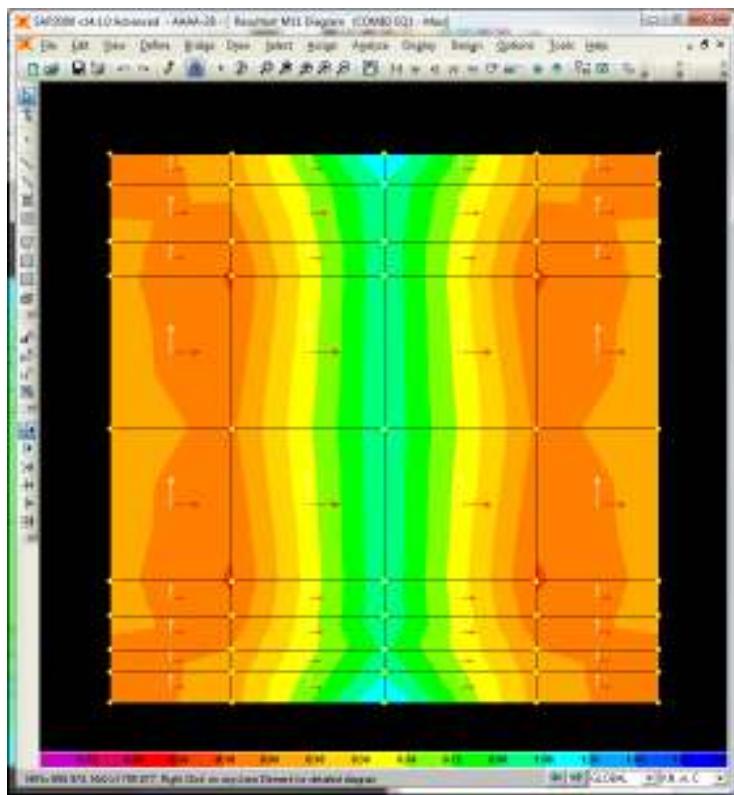


Fig Aiii-23; Bending moment distribution – Pile cap P5 (Com2 EQ1)

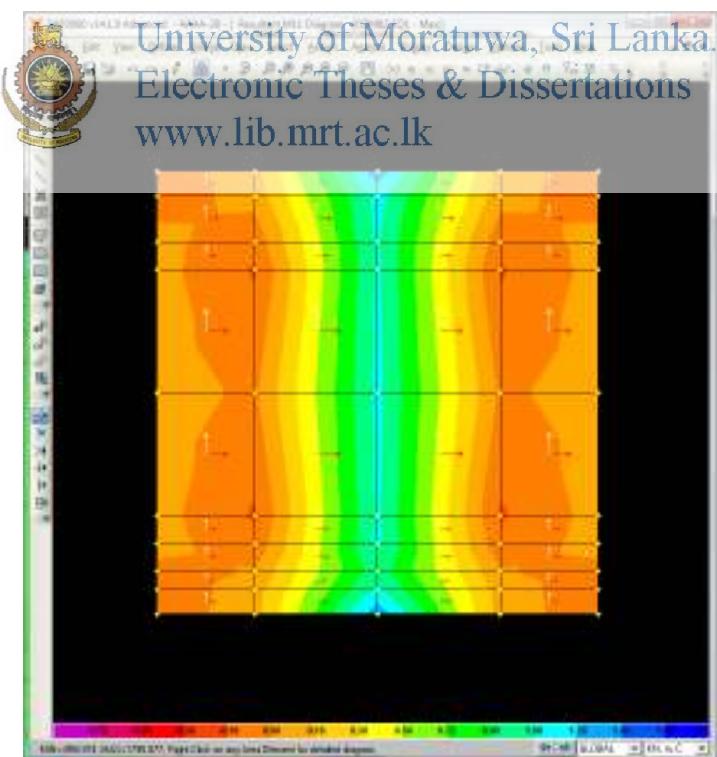


Fig Aiii-24; Bending moment distribution – Pile cap P6 (Com2 EQ1)

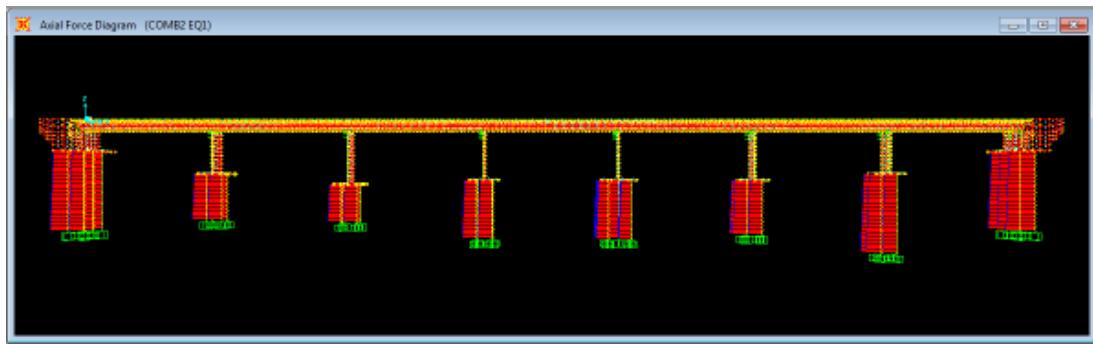


Fig Aiii-25; Axial force distribution – Piles (Com2 EQ1)

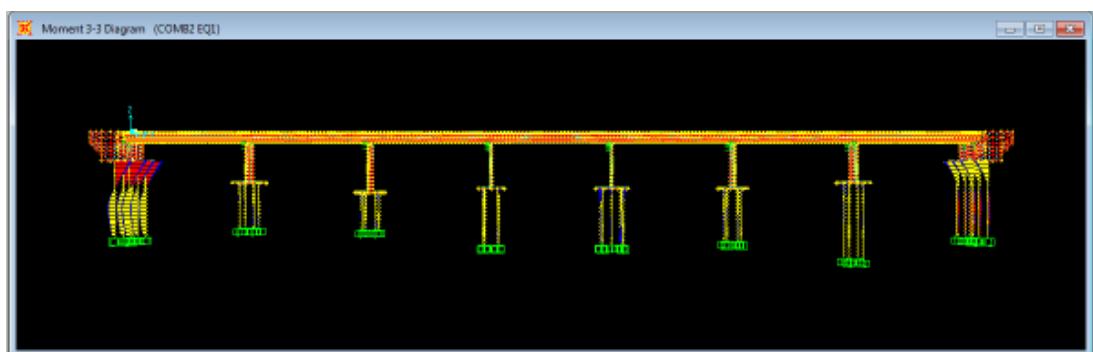


Fig Aiii-26; Bending moment distribution – Piles (Com2 EQ1)

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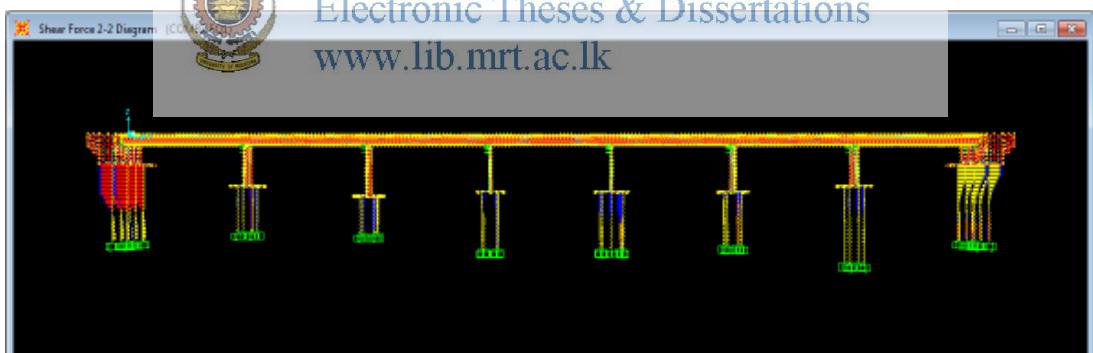


Fig Aiii-27; Shear force distribution – Piles (Com2 EQ1)

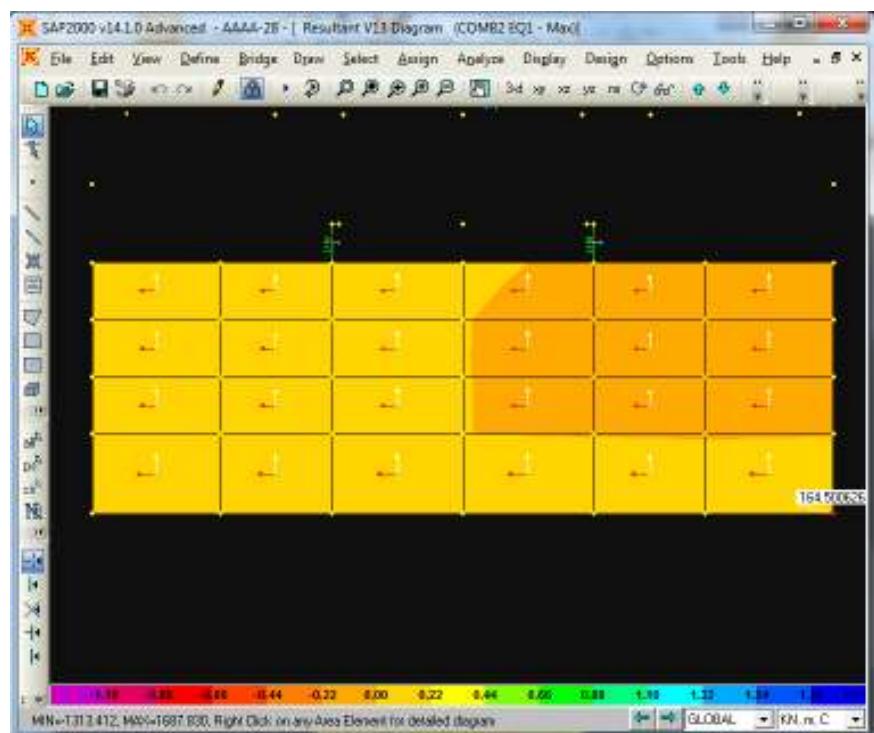


Fig Aiii-28; Shear force distribution – Abutment A1 (Com2 EQ1)

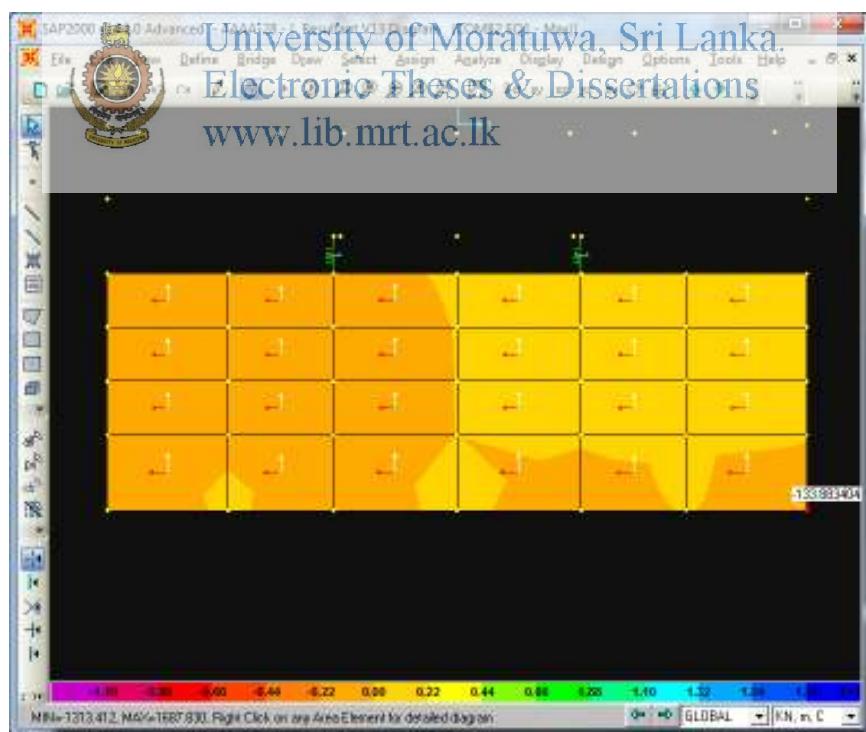


Fig Aiii-29; Shear force distribution – Abutment A2 (Com2 EQ1)

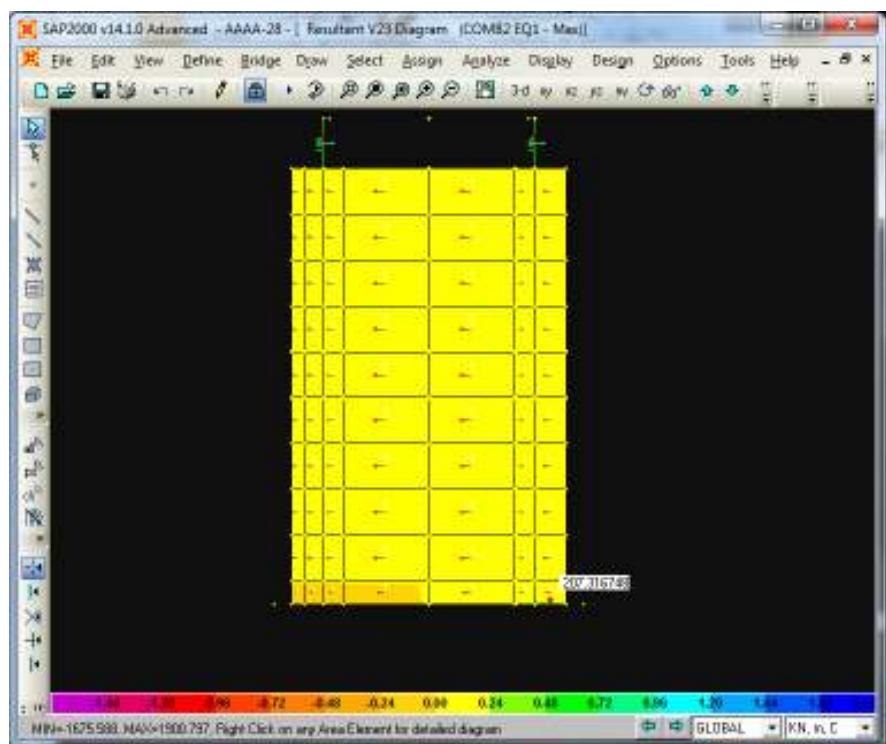


Fig Aiii-30; Shear force distribution – Pier P1 (Com2 EQ1)

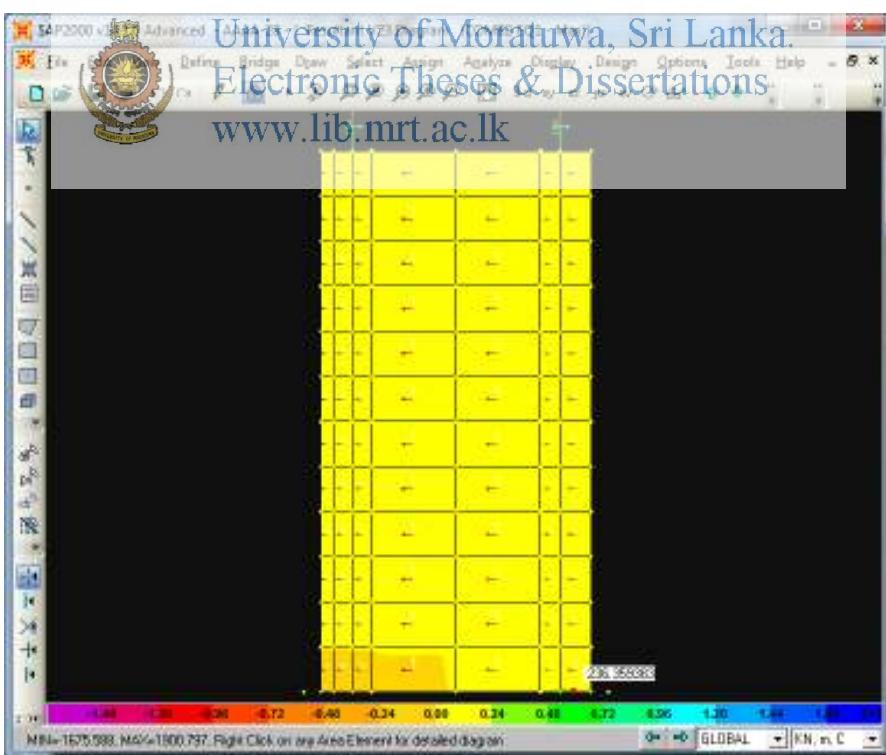


Fig Aiii-31; Shear force distribution – PierP2 (Com2 EQ1)

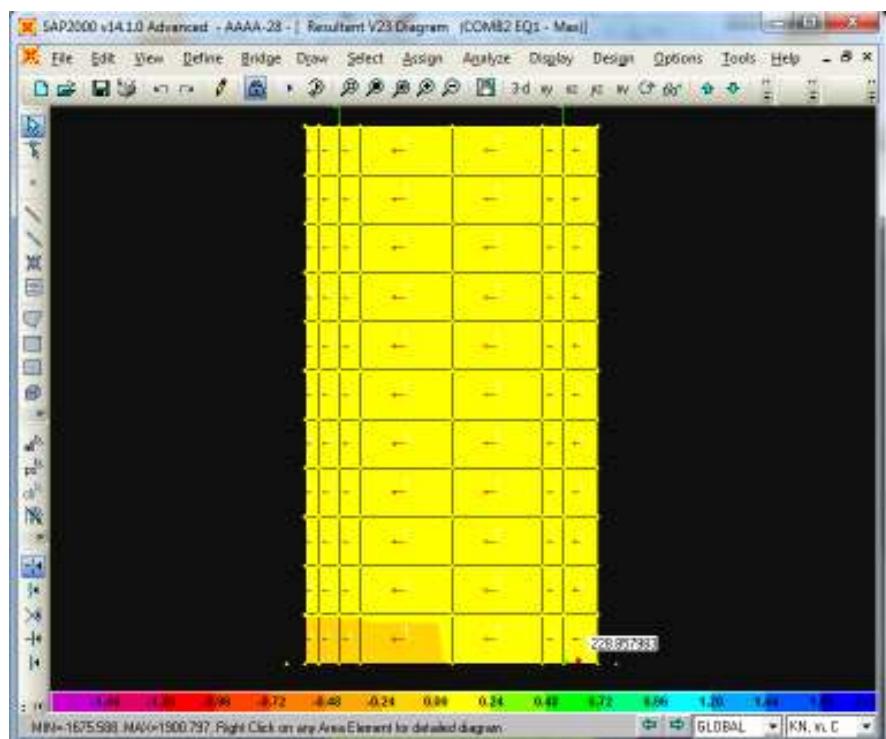


Fig Aiii-32; Shear force distribution – Pier P3 (Com2 EQ1)

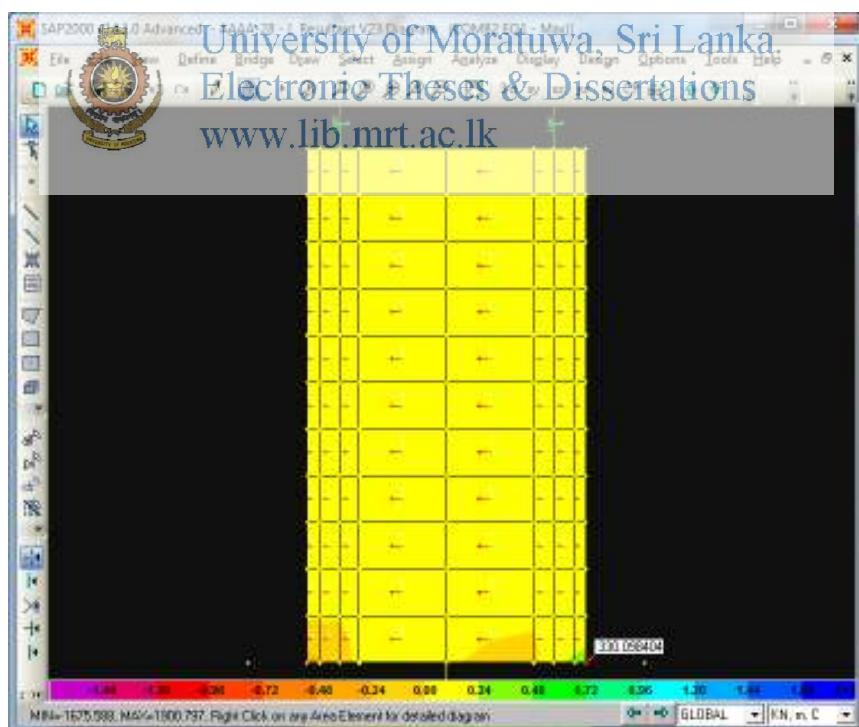


Fig Aiii-33; Shear force distribution – Pier P4 (Com2 EQ1)

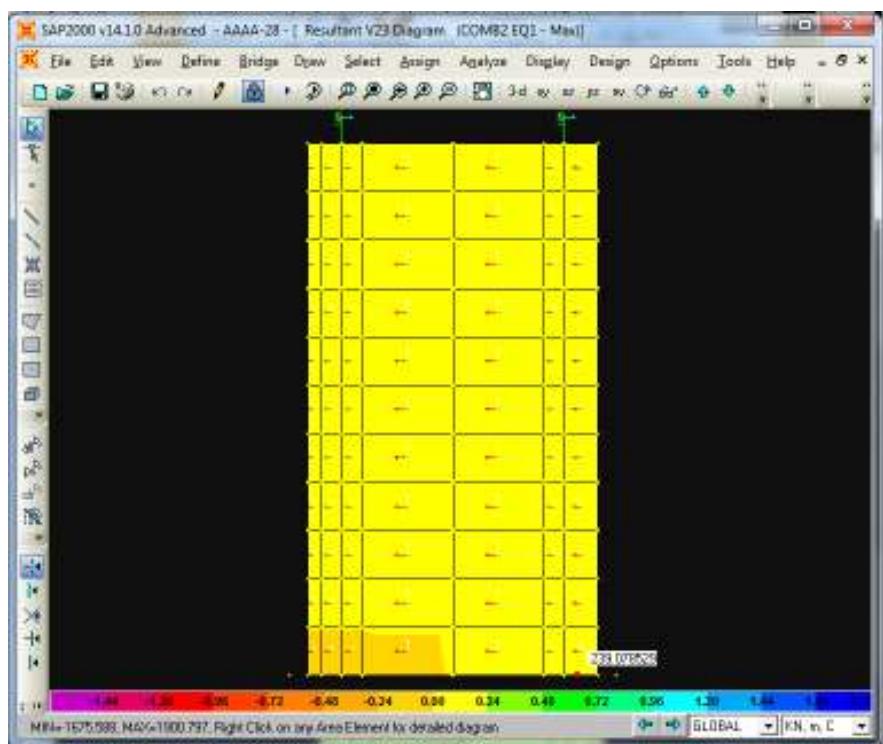


Fig Aiii-34; Shear force distribution – Pier P5 (Com2 EQ1)

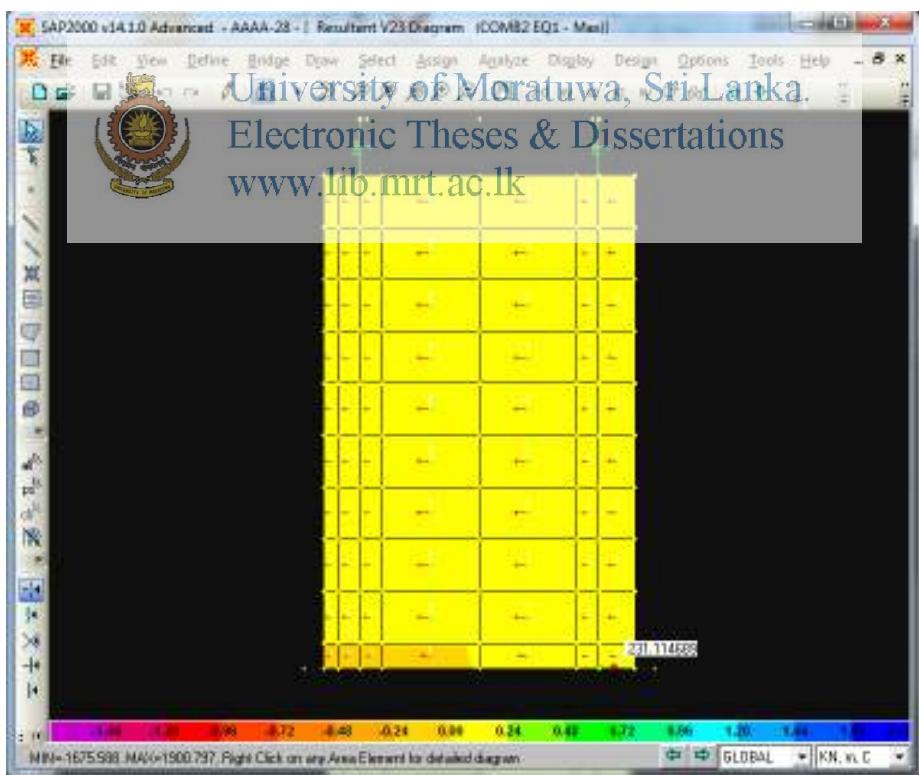


Fig Aiii-35; Shear force distribution – Pier P6 (Com2 EQ1)

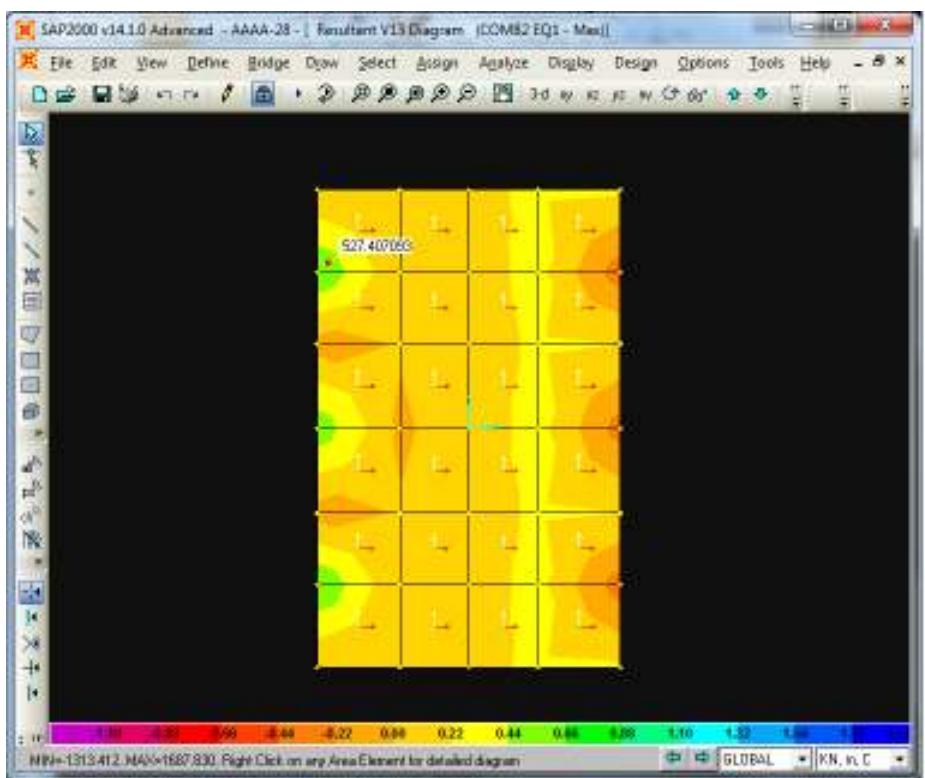


Fig Aiii-36; Shear force distribution – Pile cap A1 (Com2 EQ1)

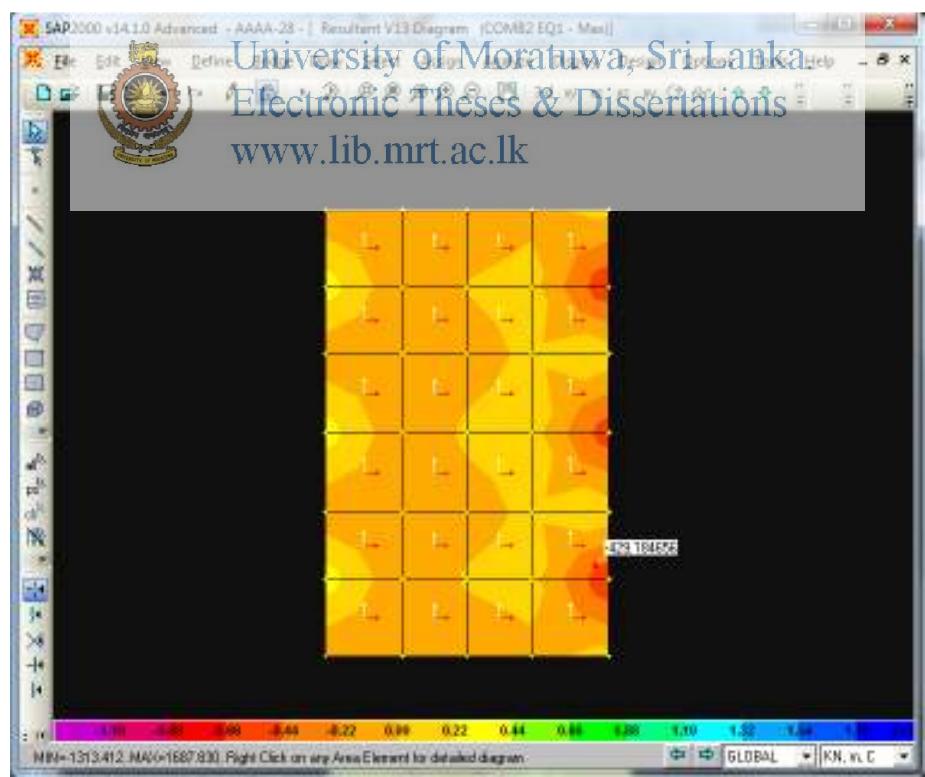


Fig Aiii-37; Shear force distribution – Pile cap A2 (Com2 EQ1)

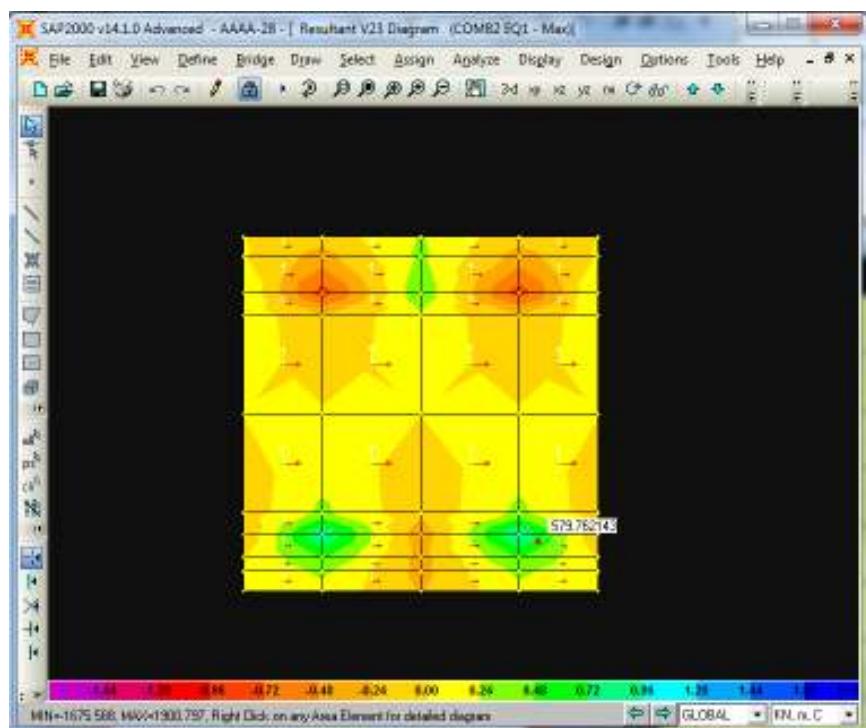


Fig Aiii-38; Shear force distribution – Pile cap P1 (Com2 EQ1)

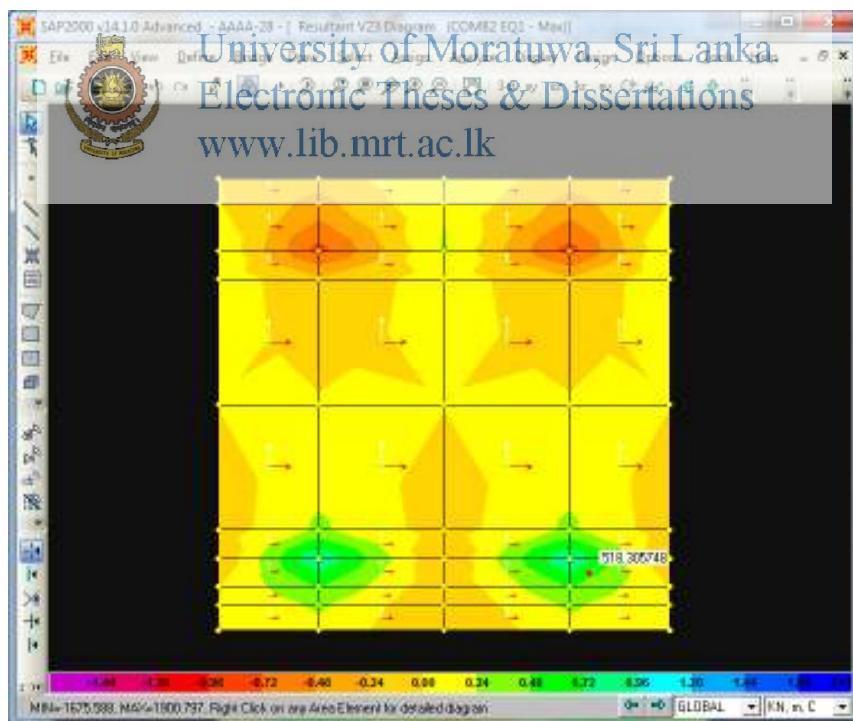


Fig Aiii-39; Shear force distribution – Pile cap P2 (Com2 EQ1)

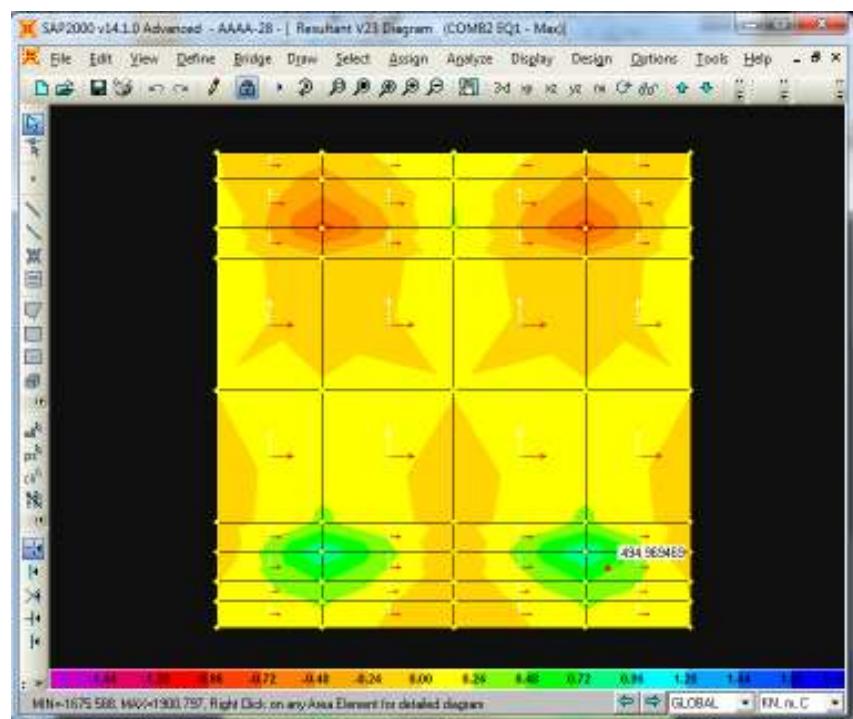


Fig Aiii-40; Shear force distribution – Pile cap P3 (Com2 EQ1)

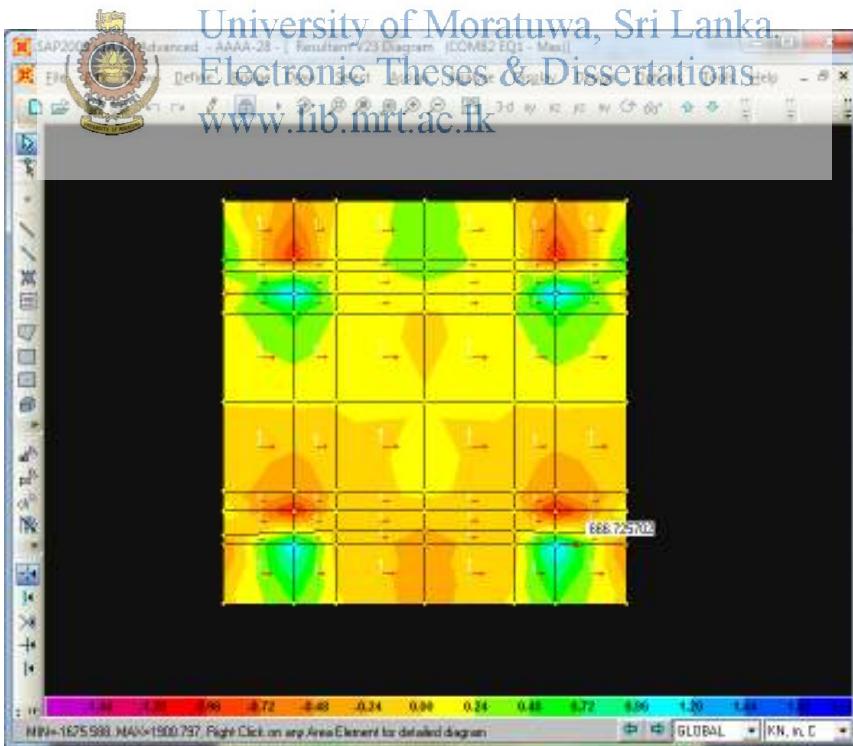


Fig Aiii-41; Shear force distribution – Pile cap P4 (Com2 EQ1)

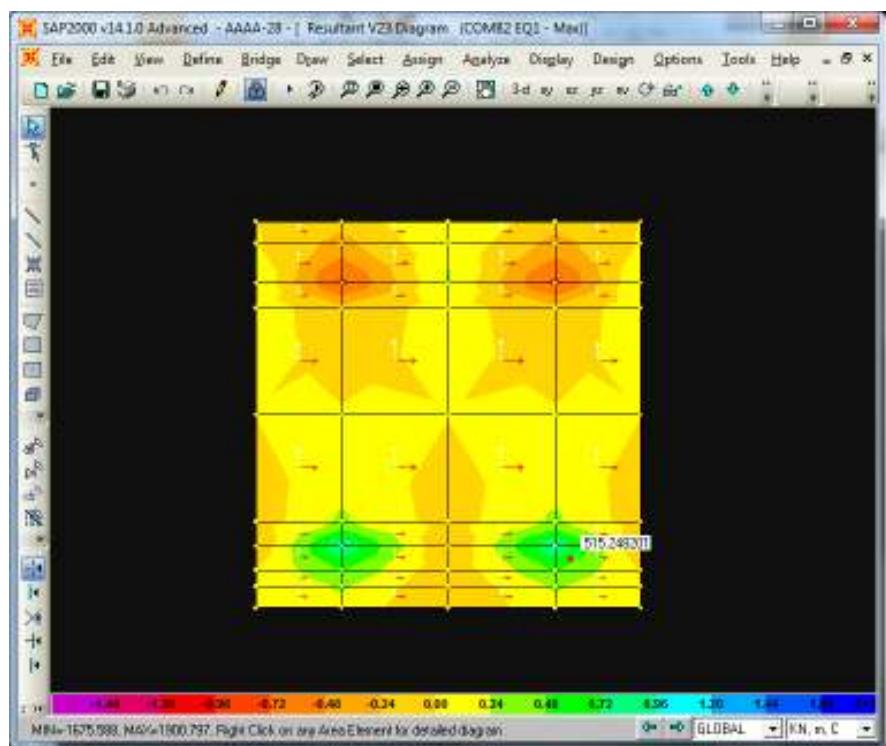


Fig Aiii-42; Shear force distribution – Pile cap P5 (Com2 EQ1)

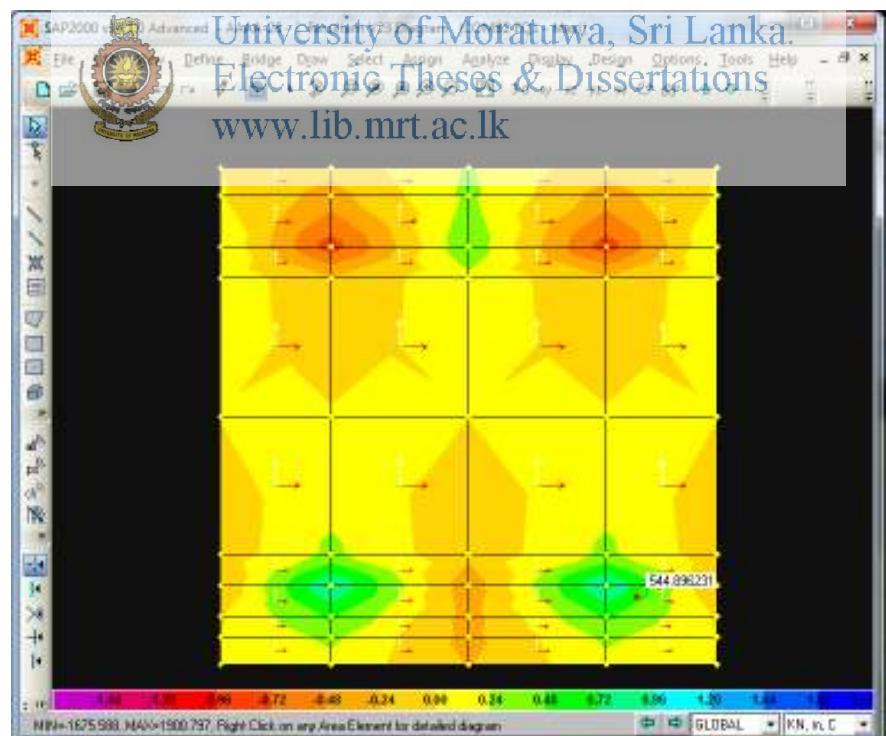


Fig Aiii-43; Shear force distribution – Pile cap P6 (Com2 EQ1)

## **APPENDIX – D**

**CAPACITY CALCULATIONS OF THE ELEMENTS**



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### **Check for Flexure for Australian Standards**

for  $k_u \leq 0.4$ , design strength in bending =  $\Phi M_{uo}$

$$M_{uo} = 1.2 \left\{ z \left( f_{cf} + \frac{P}{A_g} \right) + Pe \right\}$$

From 1st principles

$$k_u = \frac{0.003 A_s E_s}{0.85 f_c' b d \gamma} \times (1 - k_u)$$

Where,

$M_{uo}$	Ultimate strength in bending without axial forces
$Z$	Section modulus of the uncracked section
$f_{cf}$	Characteristic flexural strength of the concrete
$P$	Prestressing force
$A_g$	Gross cross sectional area of the member
$e$	Eccentricity of the prestressing force
$k_u$	Neutral axis parameter

Where  $\gamma = [0.85 - 0.007(f_c' - 28)]$

Therefore  $k_u = \frac{\sqrt{(\alpha^2 + 4\alpha)} - \alpha}{2}$



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	Stems							
	$P_1$	$P_2$	$P_3$	$P_4$	$P_5$	$P_6$	$A_1$	$A_2$
width of the section (mm)	1000	1000	1000	1000	1000	1000	1000	1000
Depth of the section (mm)	1500	1500	1500	1500	1500	1500	2150	2150
Cover to r/f (mm)	110	110	110	110	110	110	100	100
Diameter of main r/f (mm)	32	32	32	32	32	32	25	25
Spacing of the main r/f (mm)	125	125	125	125	125	125	250	250
$A_s$ Provided ( $\text{mm}^2$ )	6433.982	6433.98	6433.98	6433.98	6433.982	6433.98	1963.50	1963.50
$f_c'$ ( $\text{N/mm}^2$ )	30	30	30	30	30	30	30	30
$f_{cf}'$ ( $\text{N/mm}^2$ )	3.29	3.29	3.29	3.29	3.29	3.29	3.29	3.29
$f_y$ ( $\text{N/mm}^2$ )	340	340	340	340	340	340	340	340

$E_s$ (kN/mm <sup>2</sup> )	200	200	200	200	200	200	200	200
d (mm)	1374	1374	1374	1374	1374	1374	2037.5	2037.5
$\gamma$	0.836	0.836	0.836	0.836	0.836	0.836	0.836	0.836
$\alpha$	0.13	0.13	0.13	0.13	0.13	0.13	0.03	0.03
$k_u$	0.30	0.30	0.30	0.30	0.30	0.30	0.15	0.15
	< 0.4	< 0.4	< 0.4	< 0.4	< 0.4	< 0.4	< 0.4	< 0.4
I	1.25E+11	1.3E+11	1.3E+11	1.3E+11	1.25E+11	1.3E+11	1.8E+11	1.79E+11
$d_{NA}$	500	500	500	500	500	500	500	500
Z	2.5E+08	2.5E+08	2.5E+08	2.5E+08	2.5E+08	2.5E+08	3.6E+08	8
P	0	0	0	0	0	0	0	0
e	0	0	0	0	0	0	0	0
$A_g$	1500000	1500000	1500000	1500000	1500000	1500000	2150000	2150000
$M_{uo}$	985.9006	985.901	985.901	985.901	985.9006	985.901	1413.12	1413.124
$\phi$	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8
$\phi M_{uo}$	788.7205	788.72	788.72	788.72	788.7205	788.72	1130.5	1130.499
$M_{applied}$	424.00	423.00	418.00	320.00	410.00	428.00	246.00	214.00
	Safe	Safe	Safe	Safe	Safe	Safe	Safe	Safe



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	Pile Caps							
	P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>6</sub>	A <sub>1</sub>	A <sub>2</sub>
width of the section (mm)	1000	1000	1000	1000	1000	1000	1000	1000
Depth of the section (mm)	2000	2000	2000	2000	2000	2000	2000	2000
Cover to r/f (mm)	100	100	100	100	100	100	100	100
Diameter of main r/f(mm)	29	29	29	32	29	29	25	25
Spacing of the main r/f(mm)	125	125	125	125	125	125	250	250
A <sub>s</sub> Provided (mm <sup>2</sup> )	5284.16	5284.16	5284.16	6433.98	5284.16	5284.16	1963.50	1963.50
f <sub>c</sub> ' (N/mm <sup>2</sup> )	30	30	30	30	30	30	30	30
f <sub>cf</sub> ' (N/mm <sup>2</sup> )	3.29	3.29	3.29	3.29	3.29	3.29	3.29	3.29
f <sub>y</sub> (N/mm <sup>2</sup> )	340	340	340	340	340	340	340	340
E <sub>s</sub> (kN/mm <sup>2</sup> )	200	200	200	200	200	200	200	200
d (mm)	1885.5	1885.5	1885.5	1884	1885.5	1885.5	1887.5	1887.5
$\gamma$	0.836	0.836	0.836	0.836	0.836	0.836	0.836	0.836
$\alpha$	0.08	0.08	0.08	0.10	0.08	0.08	0.03	0.03
k <sub>u</sub>	0.24  <0.4	0.24 0.24 <0.4	0.24 0.24 <0.4	0.27 0.27 <0.4	0.24 0.24 <0.4	0.24 0.24 <0.4	0.16	0.16
I	1.67E+11	1.7E+11	1.7E+11	1.7E+11	1.67E+11	1.7E+11	1.7E+11	1.67E+11
d <sub>NA</sub>	500	500	500	500	500	500	500	500
Z	3.33E+08	3.33E+08	3.33E+08	8	3.33E+08	8	3.33E+08	8
P	0	0	0	0	0	0	0	0
e	0	0	0	0	0	0	0	0
A <sub>g</sub>	2000000	2000000	2000000	2000000	2000000	2000000	2000000	2000000
M <sub>uo</sub>	1314.534	1314.53	1314.53	1314.53	1314.534	1314.53	1314.53	1314.534
$\phi$	0.8	0.8	0.8	0.8	0.8	0.8	0.8	0.8
$\phi M_{uo}$	1051.627	1051.627	1051.627	1051.627	1051.627	1051.627	1051.627	1051.627
M <sub>Applied</sub>	1021.00	972.00	963.00	1025.00	944.00	998.00	427.00	429.00
	Safe	Safe	Safe	Safe	Safe	Safe	Safe	Safe

### Check for Shear for Australian Standards

$$\text{Design shear strength} = \phi V_u$$

$$V_u = V_{uc} + V_{us}$$

Where,

$V_{uc}$       Shear strength excluding shear r/f

$V_{us}$       Shear strength contributed by shear r/f

$$V_{uc} = \beta_1 \beta_2 \beta_3 b_v d_0 \left[ \frac{A_{st} f_c}{b_v d_0} \right]^{\frac{1}{3}}$$

Where,

$$\beta_1 = 1.1 \left[ 1.6 - \frac{d_0}{1000} \right] \geq 1.1$$

$$\beta_2 = 1.0$$

or

$$1 - \left[ \frac{N^*}{3.5 A_g} \right] \geq 0$$

$$1 + \left[ \frac{N^*}{14 A_g} \right] \geq 0$$

for members subjected to axial tension

for members subjected to axial compression

$$\beta_3 = 1.0 \text{ or}$$



In abutments & Piers it was not used shear reinforcements. Therefore  $V_{us}$  will be zero

	Stems							
	P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>6</sub>	A <sub>1</sub>	A <sub>2</sub>
Applied Shear Force V (kN)	207	236	229	330	239	231	164	133
d <sub>0</sub> (mm)	1,374	1,374	1,374	1,374	1,374	1,374	2,038	2,038
$\beta_1$	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1
A <sub>g</sub> (mm <sup>2</sup> )	1,500,000	1,500,000	1,500,000	1,500,000	1,500,000	1,500,000	2,150,000	2,150,000
N*								
$\beta_2$	1	1	1	1	1	1	1	1
$\beta_3$	2	2	2	2	2	2	2	2
b <sub>v</sub> (mm)	1,000	1,000	1,000	1,000	1,000	1,000	1,000	1,000
f <sub>c</sub> (N/mm <sup>2</sup> )	30.0	30.0	30.0	30.0	30.0	30.0	30.0	30.0
A <sub>st</sub> (mm <sup>2</sup> )	6,434	6,434	6,434	6,434	6,434	6,434	1,963	1,963
V <sub>uc</sub> (kN)	1,571	1,571	1,571	1,571	1,571	1,571	1,376	1,376

V <sub>us</sub> (kN)	-	-	-	-	-	-	-	-
V <sub>u</sub> (kN)	1,571	1,571	1,571	1,571	1,571	1,571	1,376	1,376
φ	0.7	0.7	0.7	0.7	0.7	0.7	0.7	0.7
φV <sub>u</sub> (kN)	1,100	1,100	1,100	1,100	1,100	1,100	963	963
	Satisfy	Satisfy						
Pile caps								
P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>6</sub>	A <sub>1</sub>	A <sub>2</sub>	
Applied Shear Force V (kN)	580	518	495	667	515	545	527	429
d <sub>0</sub> (mm)	1,886	1,886	1,886	1,884	1,886	1,886	1,888	1,888
β <sub>1</sub>	1	1	1	1	1	1	1	1
A <sub>g</sub> (mm <sup>2</sup> )	2,000,000	2,000,000	2,000,000	2,000,000	2,000,000	2,000,000	2,000,000	2,000,000
N*								
β <sub>2</sub>	1	1	1	1	1	1	1	1
β <sub>3</sub>	2	2	2	2	2	2	2	2
b <sub>v</sub> (mm)	1,000	1,000	1,000	1,000	1,000	1,000	1,000	1,000
f <sub>c</sub> (N/mm <sup>2</sup> )	30.0	30.0	30.0	30.0	30.0	30.0	30.0	30.0
A <sub>st</sub> (mm <sup>2</sup> )	5,284	5,284	5,284	6,434	5,284	5,284	1,963	1,963
V <sub>uc</sub> (kN)	1,652	1,652	1,652	1,763	1,652	1,652	1,189	1,189
V <sub>us</sub> (kN)							-	-
V <sub>u</sub> (kN)	1,652	1,652	1,763	1,652	1,652	1,652	1,189	1,189
φ	0.7	0.7	0.7	0.7	0.7	0.7	0.7	0.7
φV <sub>u</sub> (kN)	1,156	1,156	1,234	1,156	1,156	1,156	832	832
	Satisfy	Satisfy						

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### Check for Flexure for British Standards

Ultimate Bending Capacity

$$M_u = 0.87 f_y A_s Z$$

Where

$$Z = \left(1 - \frac{1.1 f_y A_s}{f_{cu} b d}\right) d$$

Where,

M<sub>u</sub>      Ultimate resistance moment

f<sub>y</sub>      Yield strength of reinforcement

A<sub>s</sub>      Area of tension reinforcement

Z      Liver arm

f<sub>cu</sub>      characteristic strength of concrete

b      width of the section

d      Effective depth to tension reinforcement

Z will be selected the minimum of above

$$K = \frac{M_u}{f_{cu} b d^2}$$

	Pier shaft					Abutment		
	P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>6</sub>	A <sub>1</sub>	A <sub>2</sub>
Ultimate Bending Moment (kNm/m)	424.00	423.00	418.00	320.00	410.00	428.00	246.00	214.00
Width of the section (mm)	1000	1000	1000	1000	1000	1000	1000	1000
Depth of the section (mm)	1500	1500	1500	1500	1500	1500	2150	2150
Diameter of main r/f (mm)	32	32	32	32	32	32	25	25
cover to r/f (mm)	110	110	110	110	110	110	100	100
Strength of concrete (fcu) (N/mm <sup>2</sup> )	30	30	30	30	30	30	30	30
Strength of main r/f (fy) (N/mm <sup>2</sup> )	340	340	340	340	340	340	340	340
Effective depth -d (mm)	1374	1374	1374	1374	1374	1374	2037.5	2037.5
$K = \frac{M_u}{f_{cu} bd^2}$	0.007	0.007	0.007	0.006	0.007	0.008	0.002	0.002
Z-method I	1360.87 0.95d Z	No compression r/f required 1360.90 1305.30	No compression r/f required 1361.06 1305.30	No compression r/f required 1364.11 1305.30	No compression r/f required 1361.31 1305.30	No compression r/f required 1360.74 1305.30	No compression r/f required 2032.40 1935.63	No compression r/f required 2033.06 1935.63
	mm <sup>2</sup>	1098.14	1095.55					
Main r/f spacing @	T 32 125	32 125	32 125	32 125	32 125	32 125	25 250	25 250
A <sub>s</sub> provided	6434	6434	6434	6434	6434	6434	1963	1963
Moment Capasity	2484.21	2484.21	2484.21	2484.21	2484.21	2484.21	1124.21	1124.21
Applied Moment	424.00	423.00	418.00	320.00	410.00	428.00	246.00	214.00
	OK	OK	OK	OK	OK	OK	OK	OK

	Pile cap							
	P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>6</sub>	A <sub>1</sub>	A <sub>2</sub>
Ultimate Bending Moment (kNm/m)	1021.00	972.00	963.00	1025.00	944.00	998.00	427.00	429.00
Width of the section (mm)	1000	1000	1000	1000	1000	1000	1000	1000
Depth of the section (mm)	2000	2000	2000	2000	2000	2000	2000	2000
Diameter of main r/f (mm)	29	29	29	32	29	29	25	25
cover to r/f (mm)	100	100	100	100	100	100	100	100
Strength of concrete (fcu) (N/mm <sup>2</sup> )	30	30	30	30	30	30	30	30
Strength of main r/f (fy) (N/mm <sup>2</sup> )	340	340	340	340	340	340	340	340
Effective depth -d (mm)	1885.5	1885.5	1885.5	1884	1885.5	1885.5	1887.5	1887.5
$K = \frac{M_u}{f_{cu} bd^2}$	0.010	0.009	0.009	0.010	0.009	0.009	0.004	0.004
Z-method I	No compression r/f required							
0.95d	1862.39	1863.52	1863.72	1860.78	1864.16	1862.92	1877.92	1877.87
Z	1791.23	1791.23	1791.23	1789.80	1791.23	1791.23	1793.13	1793.13
mm <sup>2</sup>	1926.98	1834.50						
Main r/f spacing @	T 29	T 29	T 29	32	29	29	25	25
A <sub>s</sub> provided	125	125	125	125	125	125	250	250
Moment Capasity	2799.78	2799.78	2799.78	3406.30	2799.78	2799.78	1041.45	1041.45
Applied Moment	1021.00	972.00	963.00	1025.00	944.00	998.00	427.00	429.00
	OK							

**Check for shear for British Standards**

	Pier shaft					Abutment		
	P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>6</sub>	A <sub>1</sub>	A <sub>2</sub>
Shear force - V (kN)	207.32	236.35	228.85	330.10	239.07	231.11	164.00	133.00
Shear stress - v=V/bd (N/mm <sup>2</sup> )	0.15	0.17	0.17	0.24	0.17	0.17	0.08	0.07
Shear capacity of concrete = 0.75(f <sub>cu</sub> ) <sup>0.5</sup> (N/mm <sup>2</sup> )	4.11	4.11	4.11	4.11	4.11	4.11	4.11	4.11
	satisfy	satisfy	satisfy	satisfy	satisfy	satisfy	satisfy	satisfy
v <sub>c</sub> = $\frac{0.27}{\gamma_m} \left[ \frac{100A_s}{bd} \right]^{\frac{1}{3}} f_{cu}^{\frac{2}{3}}$	0.52	0.52	0.52	0.52	0.52	0.52	0.31	0.31
$\xi_s = (500/d)^{1/4}$	0.78	0.78	0.78	0.78	0.78	0.78	0.70	0.70
Shear capacity = $\xi_s V_c (N/mm^2)$	0.40	0.40	0.40	0.40	0.40	0.40	0.22	0.22
	Satisfy	Satisfy	Satisfy	Satisfy	Satisfy	Satisfy	Satisfy	Satisfy
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Shear force - V (kN)	P <sub>1</sub> 579.76	P <sub>2</sub> 518.31	P <sub>3</sub> 494.97	P <sub>4</sub> 666.73	P <sub>5</sub> 515.25	P <sub>6</sub> 544.90	A <sub>1</sub> 527.41	A <sub>2</sub> 429.18
Shear stress - v=V/bd (N/mm <sup>2</sup> )	0.31	0.27	0.26	0.35	0.27	0.29	0.28	0.23
Shear capacity of concrete = 0.75(f <sub>cu</sub> ) <sup>0.5</sup> (N/mm <sup>2</sup> )	4.11	4.11	4.11	4.11	4.11	4.11	4.11	4.11
	satisfy	satisfy	satisfy	satisfy	satisfy	satisfy	satisfy	satisfy
v <sub>c</sub> = $\frac{0.27}{\gamma_m} \left[ \frac{100A_s}{bd} \right]^{\frac{1}{3}} f_{cu}^{\frac{2}{3}}$	0.44	0.44	0.44	0.47	0.44	0.44	0.32	0.32
$\xi_s = (500/d)^{1/4}$	0.72	0.72	0.72	0.72	0.72	0.72	0.72	0.72
Shear capacity = $\xi_s V_c (N/mm^2)$	0.32	0.32	0.32	0.34	0.32	0.32	0.23	0.23
	Satisfy	Satisfy	Satisfy	need shear r/f	Satisfy	Satisfy	need shear r/f	need shear r/f

calculations	Output
--------------	--------

	Pier P <sub>1</sub> ,P <sub>2</sub> ,P <sub>3</sub> ,P <sub>5</sub> ,P <sub>6</sub>	Abutment A <sub>1</sub> ,A <sub>2</sub>
Bearing Length L(mm)	1000	560
Bearing width W (mm)	710	560
Bearing thickness H (mm)	104	122
Total elastomer thickness H <sub>r</sub> (mm)	96	112
Thickness of one elastomer layer H <sub>ri</sub> (mm)	16	16
Thickness of one steel layer H <sub>s</sub> (mm)	1	1
Gross plan area A (mm <sup>2</sup> )	710000	313600
Elastomer Second moment of inertia I (mm <sup>4</sup> )	64502257.5	80207727
Shape factor S		
Shear Modulus (G) (N/mm <sup>2</sup> )	0.9	0.9
Bulk modulus E <sub>c</sub> (N/mm <sup>2</sup> )	604.22	357.52

### ***Calculation stiffness to input the FEM***



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kN/  
m

Vertical Stiffness K<sub>v</sub>

$$K_v = \frac{E_c A}{H}$$

26812262.5      7007392      kN/  
m

Rotational Stiffness

K<sub>θ</sub>

$$K_\theta = \frac{EI}{H_r}$$

405.97      256.03      kN/  
m

### ***Design check for bearing pads***

#### ***Check for maximum shear strain***

$$\varepsilon_{sc} + \varepsilon_{sr} + \varepsilon_{sh} < \frac{2.6}{\sqrt{G}}$$

$\varepsilon_{sc}$

shear strain at edge of bonded surface due to loads normal to bearing surface = 6S $\varepsilon_c$

$\varepsilon_{sr}$

shear strain at edge of bonded surface due to relative rotation of bearing surface to bearing surface

$\epsilon_{sh}$

shear strain at edge of bonded surface due to force tangential to the surface or movement of the structure or both

$$\epsilon_c = \frac{N}{3A_{eff}G(1+2S^2)}$$

Where,

$$A_{eff} = A_b \left[ 1 - \frac{\delta_a}{a} - \frac{\delta_b}{b} \right]$$

N - Compressive load on a bearing at serviceability limit state

$\delta_a$ - maximum shear displacement tangential to the bearing surface in the direction of dimension "a" due to movement of the structure and tangential forces

a - plan dimension of the edge of the bonded surface of rectangular bearings parallel to the span of the bridge

$\delta_b$ - maximum shear displacement tangential to the bearing surface in the direction of dimension "b" due to movement of the structure and tangential forces

b - plan dimension of the edge of the bonded surface of rectangular bearings transverse to the span of the bridge

$$S = \frac{A_b}{Pt_e}$$



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$A_b$  - bonded surface area

P - Surface perimeter

$t_e$  - effective thickness of the individual elastomer layer in compression(due to vertical load or rotation)

$$\epsilon_{sr} = \frac{\alpha_a a^2 + \alpha_b b^2}{2t_i t}$$

$\alpha_a$  - angle of rotation parallel to the span of the bridge

$\alpha_b$  - angle of rotation transverse to the span of the bridge

$$\epsilon_{sh} = \frac{\delta_s}{t}$$

$\delta_s$ - maximum resultant vector shear displacement tangential to the bearing surface in the direction of "a" and "b"

***Check for compressive stress***

Mean compressive stress ( $N/A_b$ ) < 15Mpa

***Check for rotational limitation***

$$d_c \geq \frac{\alpha_a a + \alpha_b b}{3}$$

where,

$$d_c = \sum (t_n \varepsilon_c)$$

$t_n$  - layer thickness of elastomer

$$\varepsilon_c = \frac{N}{EA_b} \quad \text{compressive strain of a layer}$$

$$E = E_h + \left[ \frac{C_1 GS^2}{1 + \left( \frac{C_1 GS^2}{0.75 B} \right)} \right]$$

$$E_h = 4G \left[ 1 + \left( \frac{q}{1+q} \right)^2 \right]$$

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$$C_1 = 4 + q(6 - 3.3q)$$

$q = a/b$  or  $b/a$  whichever is the lesser

***check for stability***

$$N \leq \frac{2b_e G S A_{eff}}{3t}$$

where,

$b_e$  - lesser of a and b

	Pier P <sub>1</sub> ,P <sub>2</sub> ,P <sub>3</sub> ,P <sub>5</sub> ,P <sub>6</sub>	Abutment A <sub>1</sub> ,A <sub>2</sub>
Size of the bearing	710 X 1000	560 X 560
thickness of the bearing (mm)	104	122
Inner layer thickness (mm)	16	16
No of inner layers	4	5
Steel layer thickness (mm)	1	1
Outer layer thickness (mm)	16	16
Hardness (IRHD)	60	60
Shear Modulus (G) (N/mm <sup>2</sup> )	0.9	0.9
Bulk Modulus (B) (N/mm <sup>2</sup> )	3,619	1,579
N (kN)	710,000	313,600
A <sub>b</sub> (mm <sup>2</sup> )	3420	2240
P (mm)	16	16
t <sub>c</sub> (mm)	12.975	8.750
S	1000	560
a (mm)	4.2	13.3
δ <sub>a</sub> (mm)	710	560
δ <sub>b</sub> (mm)	0	0
δ <sub>s</sub> (mm)	4.200	13.300
A <sub>eff</sub> (mm <sup>2</sup> )	707018	306152
ε <sub>c</sub>	0.0056	0.0124
ε <sub>sc</sub>	0.437	0.651
α <sub>a</sub> (rad)	0.0025	0.0025
α <sub>b</sub> (rad)	0	0
ε <sub>sr</sub>	0.7512	0.2008
ε <sub>sh</sub>	0.0404	0.1090

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$\varepsilon_{sc} + \varepsilon_{sr} + \varepsilon_{sh}$	1.2286	0.9605
2.6/G	2.9	2.9
	<b>shear strain OK</b>	<b>shear strain OK</b>
N/A <sub>b</sub> (Mpa)	5.097	5.035
	<b>Compressive stress within the limit</b>	<b>Compressiv e stress within the limit</b>
q	0.710	1.000
C <sub>1</sub>	6.596	6.700
E <sub>h</sub> (N/mm <sup>2</sup> )	4.402	4.500
E (N/mm <sup>2</sup> )	604.22	357.52
$\varepsilon_c$	0.008	0.014
( $\alpha_a a + \alpha_b b$ )/3	0.833	0.467
d <sub>c</sub>	0.810	1.577
	<b>Rotational limitations fail</b>	<b>Rotational limitations OK</b>

$$\frac{2b_e G S A_{eff}}{3t}$$



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 Stability OK Stability OK

## **APPENDIX – E**

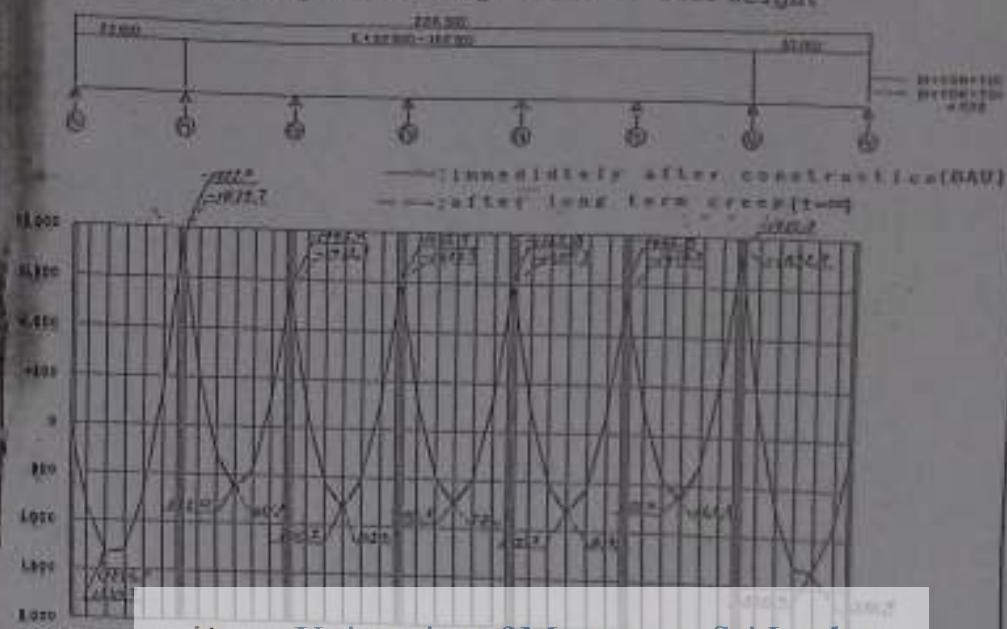
### **EXTRACTIONS OF ORIGINAL DESIGN REPORT**



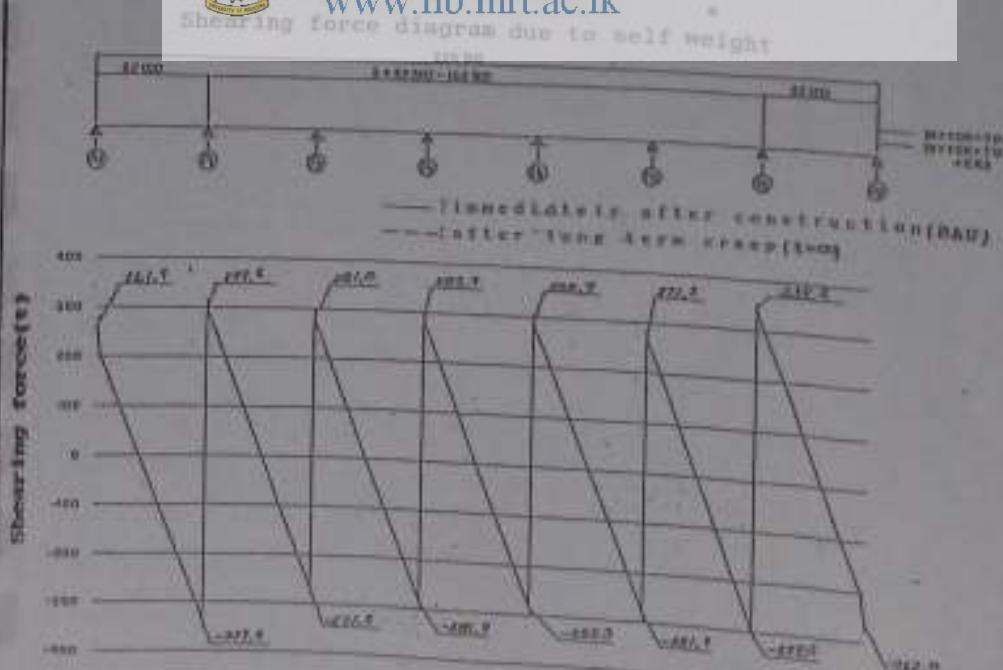
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## 3) Calculation of Sectional Forces

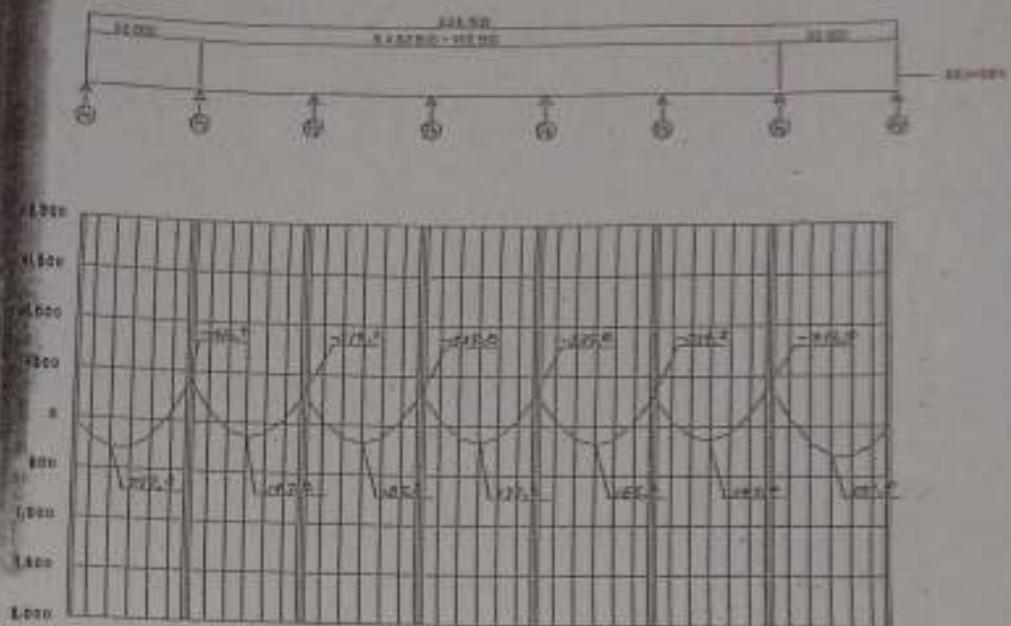
Bending moment diagram due to self weight



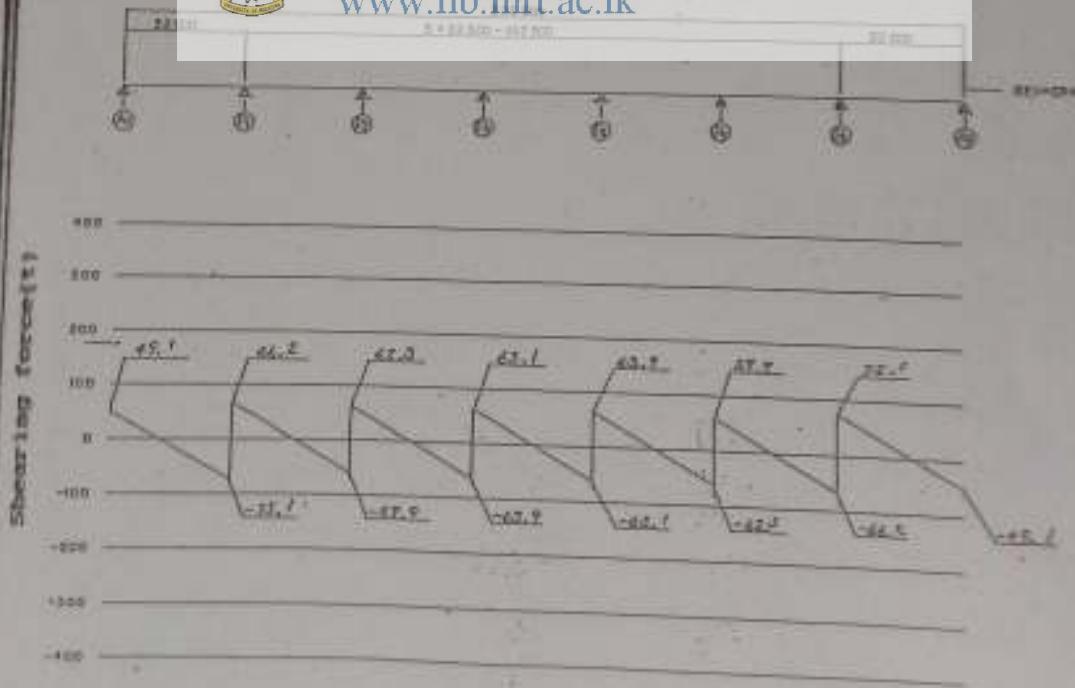
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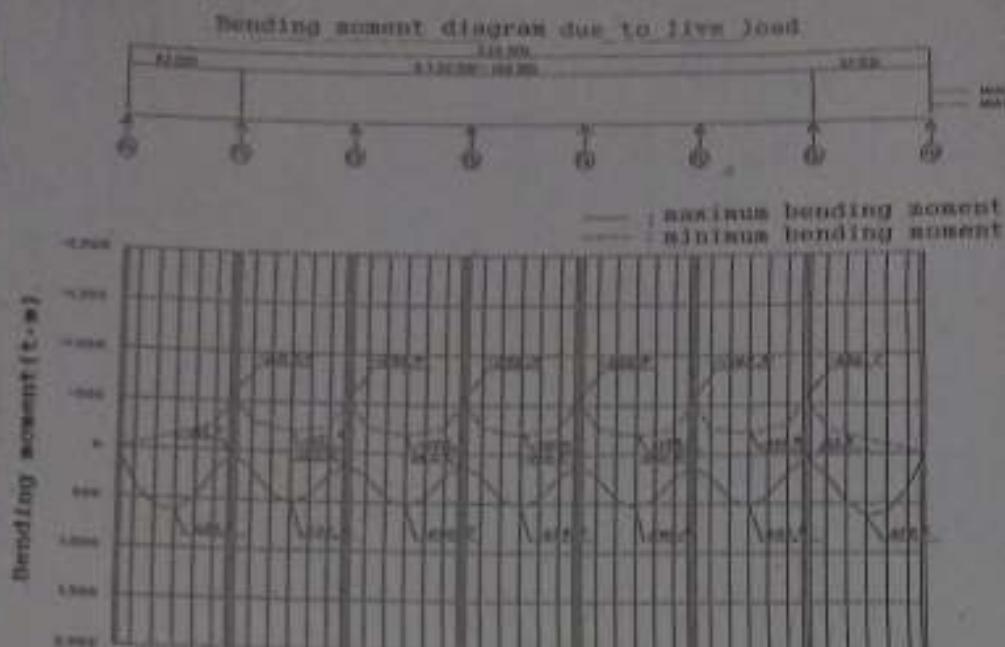
## Bending moment diagram due to superimposed dead load



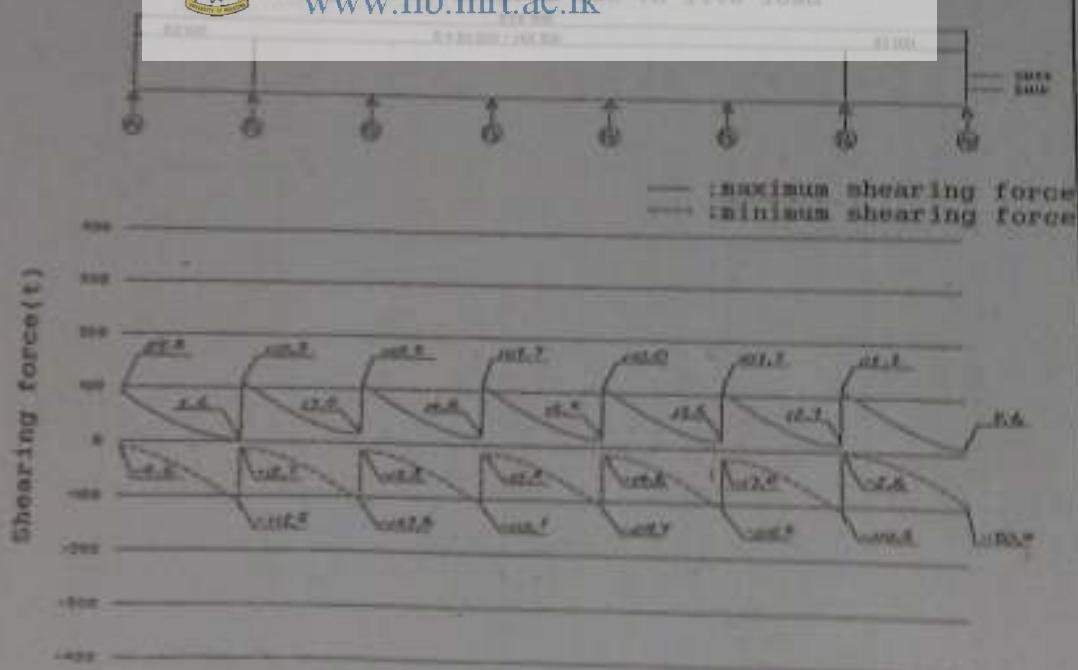
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Name	$P_1$	$P_2 (P_3)$	$\lambda_{1(A)}$
Reaction force	70 N	262 N	1.67
Vertical force	70 N	262 N	1.25
Horizontal force	20 N	93.8 N	0.37
Total	100 N	358 N	1.25

Dimensions	$P_1$	$P_2 (P_3)$	$\lambda_{1(A)}$
Base diameter	70 N	262 N	1.67
Base thickness	20 N	93.8 N	0.37
Total thickness	20 N	93.8 N	1.25

Reactions at Pile Cap	$P_1$	$P_2 (P_3)$	$\lambda_{1(A)}$
Vertical force	70 N	262 N	1.67
Horizontal force	20 N	93.8 N	0.37
Total	100 N	358 N	1.25

Soil resistance at Pile Cap	$P_1$	$P_2 (P_3)$	$\lambda_{1(A)}$
Vertical force	70 N	262 N	1.67
Horizontal force	20 N	93.8 N	0.37
Total	100 N	358 N	1.25

Soil resistance at Pile Top	$P_1$	$P_2 (P_3)$	$\lambda_{1(A)}$
Vertical force	70 N	262 N	1.67
Horizontal force	20 N	93.8 N	0.37
Total	100 N	358 N	1.25

Soil resistance at Pile Base	$P_1$	$P_2 (P_3)$	$\lambda_{1(A)}$
Vertical force	70 N	262 N	1.67
Horizontal force	20 N	93.8 N	0.37
Total	100 N	358 N	1.25

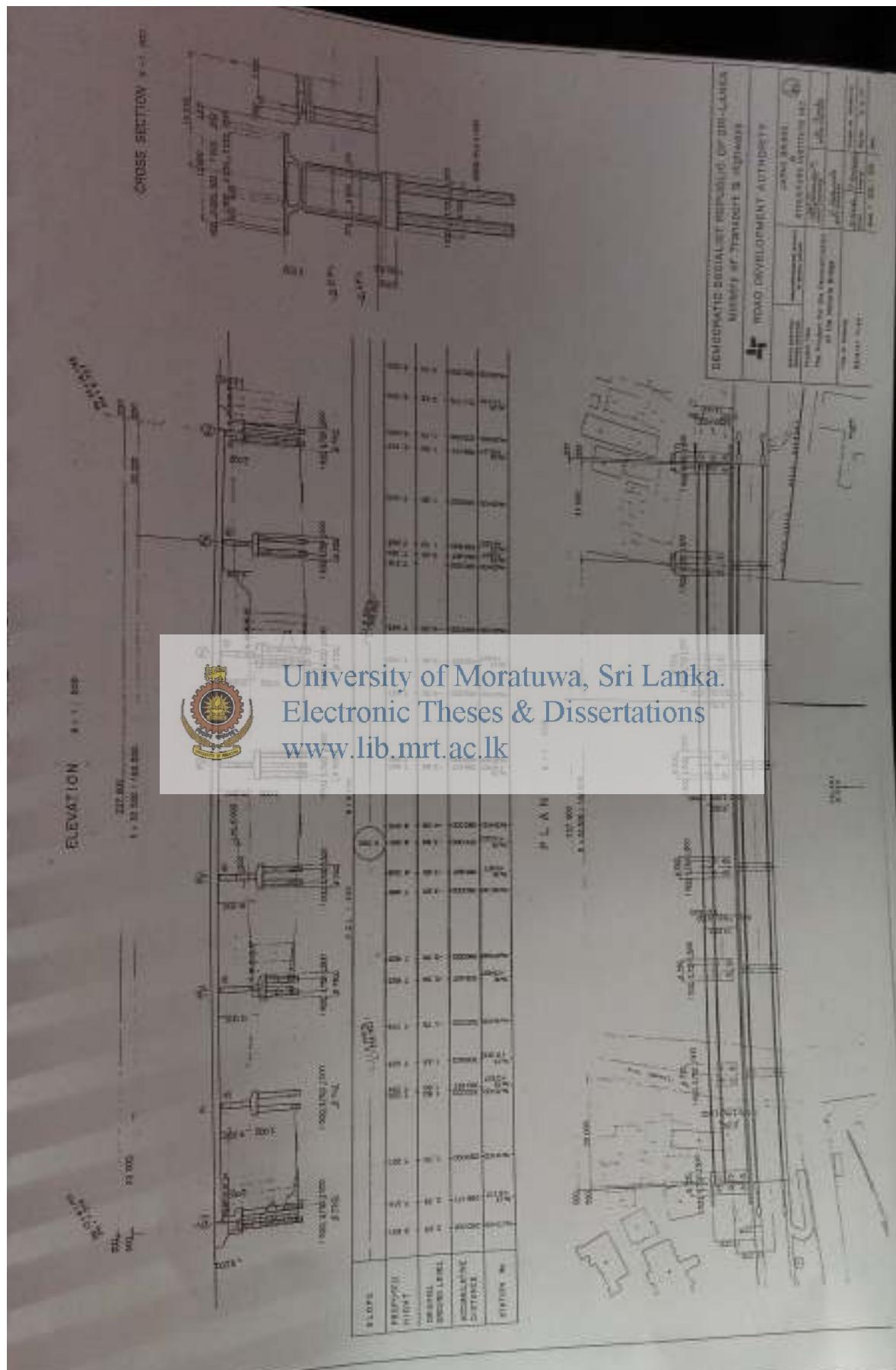
  

Soil resistance at Pile Top	$P_1$	$P_2 (P_3)$	$\lambda_{1(A)}$
Vertical force	70 N	262 N	1.67
Horizontal force	20 N	93.8 N	0.37
Total	100 N	358 N	1.25

Soil resistance at Pile Base	$P_1$	$P_2 (P_3)$	$\lambda_{1(A)}$
Vertical force	70 N	262 N	1.67
Horizontal force	20 N	93.8 N	0.37
Total	100 N	358 N	1.25

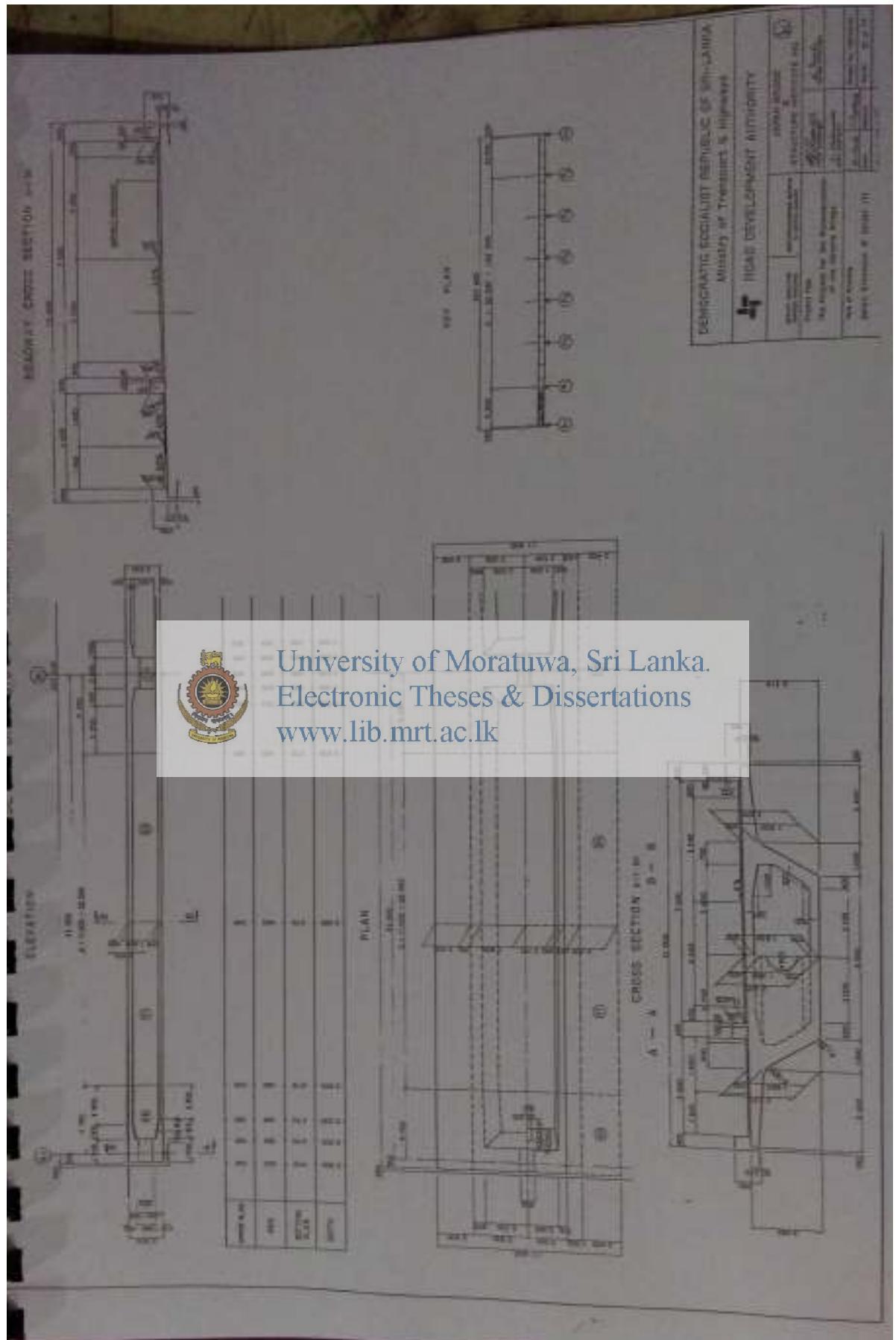
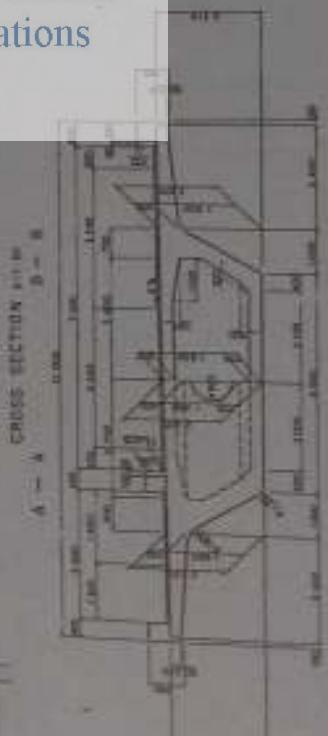




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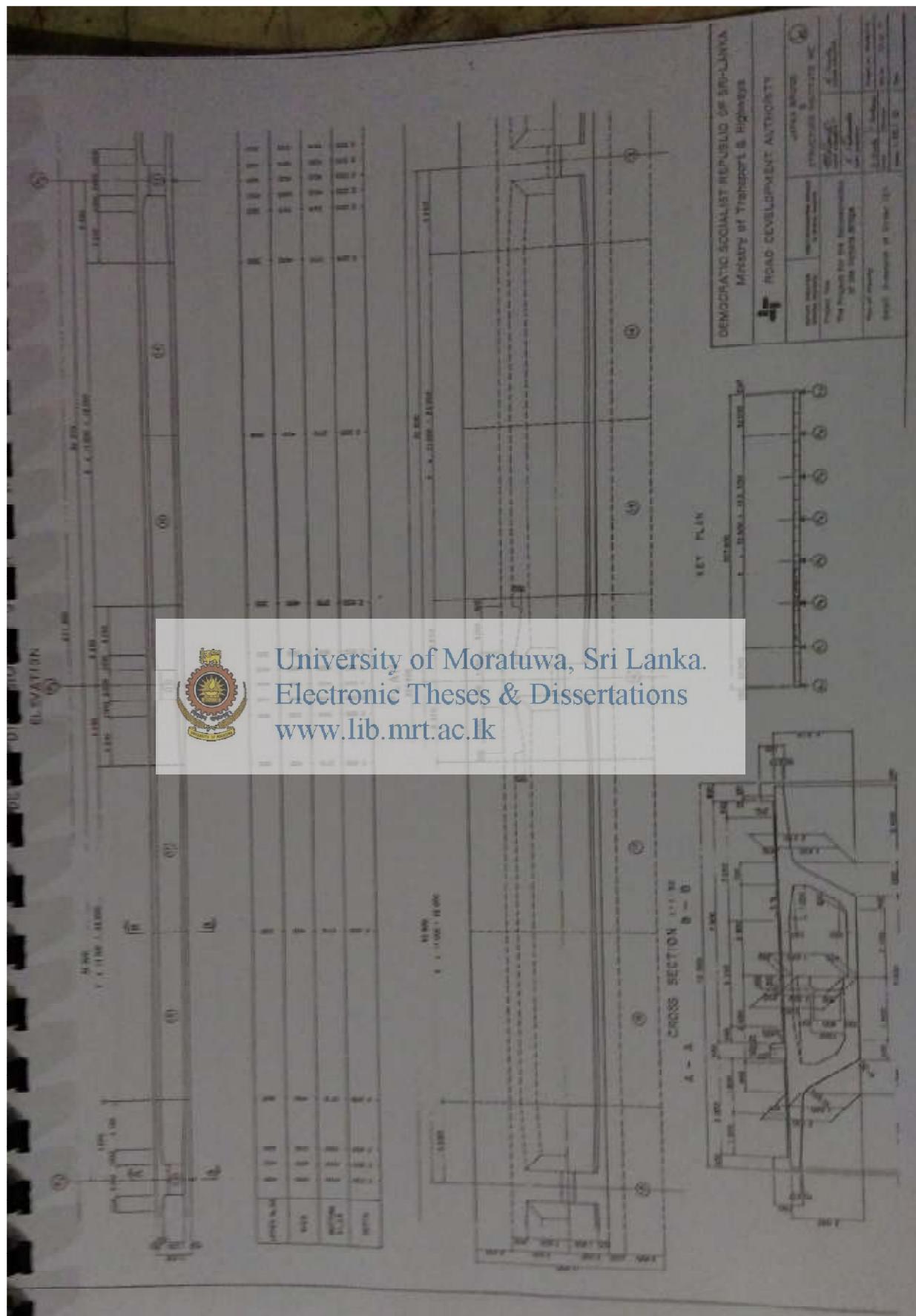


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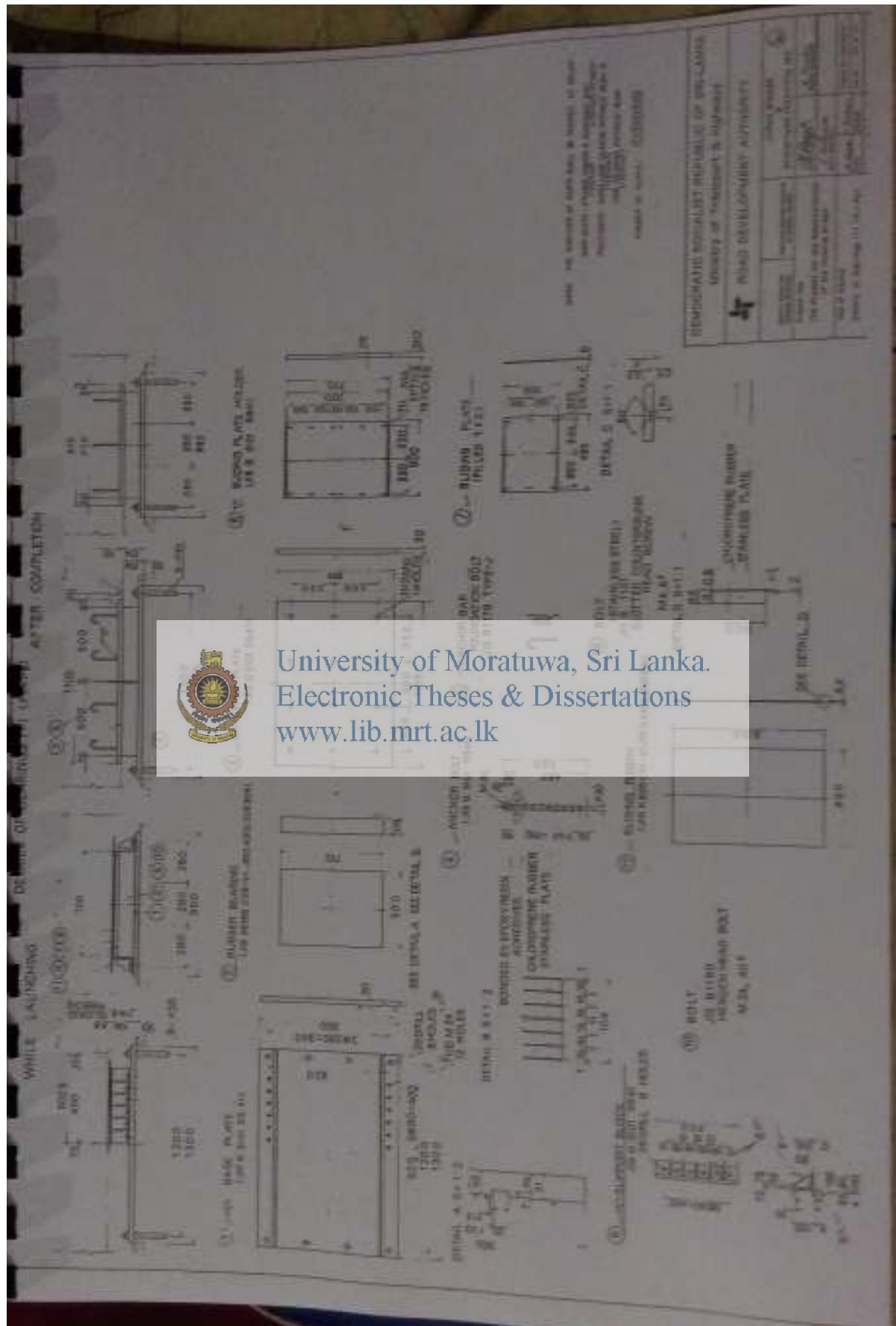


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